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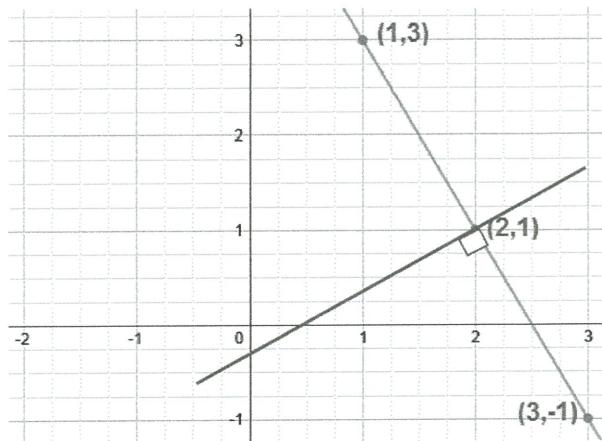
**FINAL EXAMINATION
SEMESTER I
SESI 2016/2017**

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COURSE NAME	:	MATHEMATICS I
COURSE CODE	:	BBM 10303
CODE PROGRAMME	:	BBA/BBB/BBF/BBG
DATE	:	DECEMBER 2016/JANUARY 2017
DURATION	:	3 HOURS
INSTRUCTION	:	ANSWER ALL QUESTIONS

THIS QUESTION PAPER CONSISTS OF FIVE (5) PAGES

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Q1**Figure Q1**

- (a) Find the midpoint of the line segment from point (1, 3) and point (2, 1). (2 marks)
- (b) Find the length of the line segment with the point (1, 3) and point (3, -1). (2 marks)
- (c) Find the slope of the line by going from point (1, 3) and point (2, 1). (2 marks)
- (d) Find the equation of the straight line from point (1, 3) and point (3, -1). (4 marks)
- (e) Find the equation of the straight line that passes through the point (2, 1) and is perpendicular to the straight line from point (1, 3) and point (3, -1). (4 marks)
- (f) Graph the equation of $y = \frac{1}{4}x + 5$ for domain $-2 \leq x \leq 2$. (6 marks)

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Q2 (a) Find the factors for the following quadratic equations:

(i) $x^2 - 81 = 0$

(ii) $x(2x - 5) = 12$

(iii) $2t^2 - 5t = 3$

(9 marks)

(b) Graph the quadratic equation for $y = -3x^2 - 3x - 3$.

(5 marks)

(c) Graph the equation of $y = -2x^2 + 5x - 1$ and $x = \frac{5}{4}$.

(6 marks)

Q3 (a) Solve each of the following inequalities:

(i) $4x + 3 \geq 2(3x - 1)$

(ii) $| -3x - 1 | \geq 5$

(6 marks)

(b) Express $\frac{2x+16}{x^2+x-6}$ in partial fractions.

(4 marks)

(c) If $Q(3, -4)$ be a point on the terminal side of an angle θ . Find the value of the following:

(i) $\sin \theta$

(ii) $\cos \theta$

(iii) $\tan \theta$

(6 marks)

(d) Prove that $\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta} = 1 + \tan \theta + \cot \theta$.

(4 marks)

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- Q4** (a) If $A = \begin{bmatrix} 7 & 1 & 3 \\ 8 & -2 & 7 \\ 9 & 3 & 6 \end{bmatrix}$, then find the inverse of A .
(4 marks)

(b) Solve the following equation using Gauss Elimination method:

$$x + 2y + 3z = 0$$

$$2x + 5y + 3z = 0$$

$$x + 8z = 0$$

(6 marks)

(c) Simplify $(2+i)(3-4i)$ in the form of $a+ib$.

(2 marks)

(d) Rewrite the quotient $\frac{3-7i}{2+6i}$ in standard form.

(3 marks)

(e) If $z = \sqrt{8}\left(\cos\frac{7\pi}{4} + i\sin\frac{7\pi}{4}\right)$, by using De Moivre's Theorem, find z^8 .

(5 marks)

- Q5** (a) Given $\mathbf{u} = i - 3j + 7k$ and $\mathbf{v} = 8i - 2j - 2k$, determine the following expressions:

(i) $\mathbf{u} \cdot \mathbf{v}$

(ii) $\mathbf{u} \times \mathbf{v}$

(iii) the angle between \mathbf{u} and \mathbf{v}

(6 marks)

(b) Given $\mathbf{a} = 3i - 2j + 3k$, $\mathbf{b} = j - 4k$ and $\mathbf{c} = 2i + 4j + 6k$. Find:

(i) $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})$

(ii) $(\mathbf{a} \times \mathbf{b}) \times (\mathbf{b} \times \mathbf{c})$

(4 marks)

(c) Sketch the graph of $\frac{(x-1)^2}{64} + \frac{(y-8)^2}{25} = 1$ and locate the foci.

(5 marks)

-END OF QUESTIONS-

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LIST OF FORMULA

Linear equations:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\left(\bar{x}, \bar{y} \right) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Quadratic equation:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Trigonometry:

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$\cot^2 \theta + 1 = \csc^2 \theta$$

$$\sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$$

Solution of Systems of linear:

$$A_{ij} = (-1)^{i+j} M_{ij}$$

Complex Numbers:

$$i^2 = -1$$

$$z = r e^{i(\theta+2k\pi)}$$

Vectors:

$$|v| = \sqrt{v_1^2 + v_2^2 + v_3^2}$$

Conic sections:**Circle:**

$$x^2 + y^2 = r^2$$

$$(x-h)^2 + (y-k)^2 = r^2$$

Ellipse:

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1}, x_2 \neq x_1$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$$

$$\tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha} \quad AA^{-1} = A^{-1}A = I$$

$$x_1 = \frac{|D_{x1}|}{|D|}, x_2 = \frac{|D_{x2}|}{|D|}, x_3 = \frac{|D_{x3}|}{|D|}$$

$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$\cos \theta = \frac{a \cdot b}{|a||b|}$$

Parabola:

$$x^2 = 4py$$

$$\text{Vertical: } (x-h)^2 = 4p(y-k)$$

$$\text{Horizontal: } (y-k)^2 = 4p(x-h)$$

Hyperbola:

$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

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