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UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
SEMESTER 1
SESSION 2019/2020**

COURSE NAME : ENGINEERING MATHEMATICS I
COURSE CODE : BDA 14003
PROGRAMME CODE : BDD
EXAMINATION DATE : DECEMBER 2019/JANUARY 2020
DURATION : 3 HOURS
INSTRUCTION : ANSWER FIVE (5) QUESTIONS ONLY

THIS QUESTION PAPER CONSISTS OF **THREE (3)** PAGES

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Q1 (a) Solve the domain and range of the following functions:

(i) $f(x) = \sqrt{6 + x - x^2}$ (5 marks)

(ii) $h(x) = \frac{10}{\sqrt{16 - x^2}}$ (5 marks)

(b) Examine the limit for the functions of :

(i) $\lim_{x \rightarrow 8} \frac{2x^2 - 17x + 8}{8 - x}$ (4 marks)

(ii) $\lim_{z \rightarrow 0} \frac{z}{3 - \sqrt{z + 9}}$ (6 marks)

Q2 (a) Calculate this function $f(x) = \sin(\sqrt{1 + \cos x})$ using the Chain Rule method (5 marks)

(b) Examine the derivative function of $x^2 \tan(y) + y^{10} \sec(x) = 2x$ using Implicit Differentiation method (7 marks)

(c) The amount of air in the balloon at any time, t is given by $v(t) = \frac{6\sqrt[3]{t}}{4t + 1}$. Find the:

(i) rate of change of the volume, $\frac{dv}{dt}$ (4 marks)

(ii) balloon being filled or drained when $t = 8$ seconds? (4 marks)

Q3 (a) Identify the suitable method for the integration of $\int_0^8 x\sqrt{1+x} dx$ (6 marks)

(b) Calculate the integrals of $\int_0^1 4x^2 e^{-2x} dx$ (8 marks)

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- (c) Examine the integral by using partial fraction method $\int \frac{x^2 + x + 3}{x + 2} dx$ (6 marks)
- Q4** (a) Solve the arc length of the graph $y = \frac{1}{3}(x^2 + 2)^{\frac{3}{2}}$ on the interval $[0,1]$ (10 marks)
- (b) Examine the area of the surface that is generated by revolving the portion of the curve $y = x^2$ between $x=1$ and $x=2$ about the y -axis (10 marks)
- Q5** (a) Let the function as $f(x) = \frac{x^2-1}{|x-1|}$
- (i) Find $\lim_{x \rightarrow 1^+} f(x)$ (5 marks)
- (ii) Find $\lim_{x \rightarrow 1^-} f(x)$ (5 marks)
- (iii) Does $\lim_{x \rightarrow 1} f(x)$ exists? (2 marks)
- (b) Use L'Hospital's Rule for the limit of $\lim_{z \rightarrow 0} \frac{\sin(2z) + 7z^2 - 2z}{z^2(z+1)^2}$ (8 marks)
- Q6** (a) Solve the integral $\int \sqrt{5 - 4x - x^2}$ by using trigonometry substitution method (10 marks)
- (b) Solve the volume of the solid that is obtained when the region under the curve $y = \sqrt{x}$ over the interval $[1, 4]$ is revolved at about 90° , 180° , 270° and 360° of the x -axis (10 marks)