

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

FINAL EXAMINATION SEMESTER II SESSION 2014/2015

COURSE NAME : ENGINEERING TECHNOLOGY

MATHEMATICS II

COURSE CODE : BDU 11003

PROGRAMME : 1 BDU

EXAMINATION DATE : JUNE/JULY 2015

DURATION : 3 HOURS

INSTRUCTION : A) ANSWER ALL QUESTIONS

IN SECTION A

B) ANSWER TWO

QUESTIONS ONLY IN

SECTION B

THIS QUESTION PAPER CONSISTS OF SIX (6) PAGES

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SECTION A

Q1 (a) Obtain the particular solution for the differential equation

$$q\frac{dp}{dq} - 3 = 2\left((p + \frac{dp}{dq})\right),$$

which satisfies the initial condition p(3) = 0.

(5 marks)

(b) Find the particular solution for the differential equation

$$2\ddot{U} - 2\dot{U} + U = 0$$
, $U(0) = 1$, $\dot{U}(0) = 1$. (5 marks)

(c) A metal object is heated to 200°C and then placed in a large room to cool. The temperature of the room is held constant at 20°C. After 10 min, the object's temperature is 100°C. How long will it take the object to cool to 25°C?

(5 marks)

(d) For population of about 100,000 bacteria in a petri dish, we decide to model population growth by the differential equation

$$\frac{dP}{dt} = kP.$$

Suppose, 2 days later, that the population has grown to about 150,000 bacteria. Find the growth rate k and estimate the bacteria population after 7 days.

(5 marks)

Q2 (a) The motion of a particle satisfies the equation

$$\frac{d^2x}{dt^2} + 2\gamma \frac{dx}{dt} + 169x = 0, \quad \gamma > 0,$$

which satisfies the initial conditions x(0) = 0 and $\dot{x}(0) = 8$.

- (i) Find the value of γ such that its characteristic equation has equal real roots and determine x in term of t.
- (ii) If $\gamma = 12$, find x in term of t.
- (iii) If $\gamma = 14$, find x in term of t.

(10 marks)

(b) Find the solution of the differential equation by using variation of parameters technique

$$\ddot{V} + 4\dot{V} + 3V = te^{-t}$$
.

which satisfies the conditions V(0) = 0 and $\dot{V}(0) = 1$.

(10 marks)

Q3 (a). Find the Laplace transforms of the following functions.

(i)
$$f(t) = 5t^3 + 6t$$
.

(4 marks)

(ii)
$$f(t) = (t+1)^3$$
.

(4 marks)

- (b). Find the inverse Laplace transforms of the following expressions.
 - (i) $\frac{s+3}{4s^2+9}$.

(6 marks)

(ii) $\frac{3s+5}{16s^2-9}$

(6 marks)

SECTION B

Q4 By using Laplace transform, solve the initial value problems

(a).
$$y' + y = \cos t$$
, $y(0) = 0$. (10 marks)

(b).
$$\ddot{p} + 4p = e^{-t}$$
, $p(0) = 2$, $\dot{p}(0) = 1$. (10 marks)

A periodic function f(x) is defined by **Q5**

$$f(x) = \begin{cases} 1, & -1 < x < 0, \\ 3, & 0 < x < 1, \end{cases}$$

and

$$f(x) = f(x+2).$$

Sketch the graph of the function over -3 < x < 3. (i)

(3 marks)

Find the Fourier coefficients corresponding to the function. (ii)

(10 marks)

following function and ... $g(t) = e^t, \ 0 \le t < 1, \text{for a large state of the st$ (b). Sketch the graph of the following function and find the Laplace transforms.

$$g(t) = e^t$$
, $0 \le t < 1$,

$$g(t) = g(t+1).$$

Q6 (a) Use the method of separation of variables to solve the following initial-boundary value problem

PDE:
$$\frac{\partial u}{\partial t} = 3 \frac{\partial^2 u}{\partial x^2}$$

Boundary conditions: $u(0,t) = u(\pi,t) = 0$, (t > 0),

Initial conditions:
$$u(x, 0) = x(\pi - x), (0 < x < \pi).$$

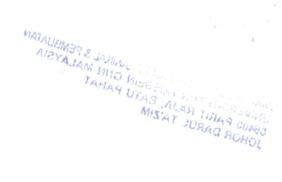
(10 marks)

(b) By using undetermined coefficients technique, find the solution of the differential equation

$$\ddot{y} - 2\dot{y} + y = 2x^2 - 1$$
, $y(0) = 1$ and $\dot{y}(0) = 2$.

(10 marks)

- END OF QUESTION -



FINAL EXAMINATION

SEMESTER/SESSION : SEM 2/2014/2015 COURSE NAME : ENG. TECH. MATH. 2 PROGRAMME: 1 BDD COURSE CODE: BDU11003

Formulae

f(x)	$y_p(x)$
$P_n = A_n x^n + A_{n-1} x^{n-1} + \dots + A_0$	$x^{r}(B_{n}x^{n} + B_{n-1}x^{n-1} + \dots + B_{0})$
$Ce^{\lambda x}$	$x^r(Ke^{\lambda x})$
$C \cos \omega x \text{ or } D \sin \omega x$	$x^r(k\cos\omega x + l\sin\omega x)$
$C\cos\omega x + D\sin\omega x$	
$W = \begin{vmatrix} y_1 & y_2 \\ y'_1 & y'_2 \end{vmatrix}, u = -\int \frac{y_2 f(x)}{aW} dx = A$	$v = \int \frac{y_1 f(x)}{aW} dx + B$
$u(x,t) = \sum_{n=1}^{\infty} D_n \sin\left(\frac{n\pi x}{l}\right) e^{-\frac{n^2 \pi^2 k^2 t}{l^2}}$	$D_n = \frac{2}{l} \int_0^l f(x) \sin\left(\frac{n\pi x}{l}\right) dx, n = 1,2,3,$

f(t)	F(s)	Condition on s
а	a/s	s > 0
$t^n, n = 0,1,2,$	$n!/s^{n+1}$	s > 0
e ^{at}	_1	s > 0
	s-a	100
sin at	$\frac{a}{s^2 + a^2}$	s > 0
cos at	$\frac{s}{s^2 + a^2}$	SI > 0
sinh at	$\frac{a}{s^2 - a^2}$	s > a 24 115 ay 00
$\cosh at$	$\frac{s}{s^2 - a^2}$	s > a