

**CONFIDENTIAL**



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER II  
SESSION 2012/2013**

COURSE NAME : DYNAMICS  
COURSE CODE : BDA20103/ BDA2013  
PROGRAMME : BACHELOR OF MECHANICAL  
ENGINEERING WITH HONOURS  
EXAMINATION DATE : JUNE 2013  
DURATION : 3 HOURS  
INSTRUCTION : ANSWER ONLY **FIVE** QUESTIONS

THIS PAPER CONTAINS ELEVEN (11) PRINTED PAGES

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**ANSWER ONLY FIVE QUESTIONS**

**Q1** (a) Define two conditions of any object to be considered as a particle. (4 marks)

(b) **FIGURE Q1** shows A1 Circuit used by car A and car B for preparation before the actual championship. Car B is moving along the curved lap with a velocity  $18 \text{ ms}^{-1}$ , at the same time decelerating at  $2 \text{ ms}^{-2}$ . In front of this car, car A is travelling along the straight part of the circuit with a velocity  $35 \text{ ms}^{-1}$ , while decelerating at  $5 \text{ ms}^{-2}$  due to sudden transmission issue. At this instant, determine:

(i) the velocity of car B relative to car A,  $v_{B/A}$ . (8 marks)

(ii) the acceleration of car B with respect to car A,  $a_{B/A}$ . (8 marks)

**Q2** **FIGURE Q2** shows a cannonball A, B and C of mass 80 kg, 40 kg and 60 kg respectively. Cannonball A travels with a velocity  $20 \text{ ms}^{-1}$  just before it strikes cannonball B, which is rest horizontally. The collision causing cannonball B to hits stationary cannonball C, which then makes it move further towards the anvil wall. Suppose the restitution coefficient for collision between cannonballs A and B is 0.3 and the restitution coefficient for collision between cannonballs B and car C is 0.8, determine:

(a) the velocity of cannonball B,  $v_B$  when it hits the cannonball C. (7 marks)

(b) the velocity of cannonball C,  $v_C$  at which it strikes the anvil wall. (7 marks)

(c) the velocity of cannonball C,  $v_C$  when it rebounds from the anvil wall if restitution coefficient between them is 0.75. (6 marks)

**Q3** A wooden crate is lifted from the floor by using three pulleys system as shown in **FIGURE Q3**. The crate is connected to a pulley C by an inextensible cable. The motion of the crate, pulleys A, B and C is controlled by a cable D which move with a constant acceleration,  $a_D = 2 \text{ m/s}^2$  and an initial velocity,  $(V_0)_D = 4 \text{ m/s}$ , in the direction as shown. Pulleys A and B are of double pulley type. At time,  $t = 10$  seconds, determine:

- (a) the numbers of revolution,  $N$  rpm executed by the pulley A. (4 marks)
- (b) the angular velocity of the pulley B,  $\omega_B$  rad/s. (4 marks)
- (c) the magnitude and direction of acceleration of point E at pulley B,  $a_E$  m/s<sup>2</sup>. (4 marks)
- (d) the velocity,  $v$  m/s and the distance,  $S$  meter of the crate moved. (8 marks)

**Q4** (a) The bar AB of the linkage shown in **FIGURE Q4(a)** has a clockwise angular velocity,  $\omega = 30 \text{ rad/s}$  when  $\theta = 60^\circ$ . Using the instantaneous centers of zero velocity, determine the angular velocities,  $\omega$  (magnitude and direction) of members BC and the wheel CD at this instant.

(5 marks)

(b) At the instant shown in **FIGURE Q4(b)**, link AB has an angular velocity,  $\omega_{AB} = 2 \text{ rad/s}$  and an angular acceleration,  $\alpha_{AB} = 6 \text{ rad/s}^2$ . At instant  $\theta = 60^\circ$ , determine:

- (i) the magnitude and direction of acceleration at pin B,  $a_B$  m/s<sup>2</sup>. (2 marks)
- (ii) the angular velocity of link BC,  $\omega_{BC}$  rad/s and link CD,  $\omega_{CD}$  rad/s. (4 marks)
- (iii) the angular acceleration of link CB,  $\alpha_{CB}$  rad/s<sup>2</sup>. (5 marks)
- (iv) the angular acceleration of link CD,  $\alpha_{CD}$  rad/s<sup>2</sup>. (4 marks)

**Q5** Two homogenous steel slender rod and thin plate are welded together to form a pendulum as shown in **FIGURE Q5**. The density of the slender rod is  $1.5 \text{ kg/m}$  and the thin plate is  $10 \text{ kg/m}^2$ . Determine:

- (a) the mass of the slender rod and the thin plate. (4 marks)
- (b) the location of the center of mass,  $G$  of the pendulum. (4 marks)
- (c) the moment of inertia of the pendulum about an axis perpendicular to the page and passing through  $G$ . (6 marks)
- (d) the moment of inertia of the pendulum about an axis perpendicular to the page and passing through  $O$ . (6 marks)

**Q6** A spring having a stiffness of  $k = 600 \text{ N/m}$  is attached to the point B of the  $6 \text{ kg}$  rod, with an unstretched length of  $300 \text{ mm}$  as shown in **FIGURE Q6**. If the rod is released from rest at  $\theta = 30^\circ$  to  $\theta = 0^\circ$ ;

- (a) draw the diagram of the rod, when it is located at its initial ( $\theta = 30^\circ$ ) and final ( $\theta = 0^\circ$ ) positions. (4 marks)
- (b) calculate the total potential energy at the initial and final positions. (8 marks)
- (d) determine the angular velocity,  $\omega$  of the rod at the instant  $\theta = 0^\circ$ . (8 marks)

**JAWAB LIMA SOALAN SAHAJA**

**S1** (a) Terangkan dua keadaan yang membolehkan sesuatu objek dianggap sebagai zarah.  
(4 markah)

(b) **RAJAH S1** menunjukkan sirkit perlumbaan A1 yang digunakan oleh kereta A dan kereta B sebagai persediaan sebelum kejohanan sebenar. Kelihatan kereta B sedang bergerak di sepanjang selekoh dengan kelajuan  $18 \text{ ms}^{-1}$ , pada waktu yang sama mengalami penurunan halaju sebanyak  $2 \text{ ms}^{-2}$ . Manakala di hadapan kereta ini, kereta A sedang bergerak di sepanjang laluan tegak dengan kelajuan  $35 \text{ ms}^{-1}$ , dan turut mengalami penurunan halaju sebanyak  $5 \text{ ms}^{-2}$  disebabkan masalah enjin. Pada ketika ini, tentukan:

(i) halaju kereta B terhadap kereta A,  $v_{B/A}$ .  
(8 markah)

(ii) pecutan kereta B terhadap kereta A,  $a_{B/A}$ .  
(8 markah)

**S2** **RAJAH S2** menunjukkan peluru meriam A, B dan C dengan masing-masing berjisim 80 kg, 40 kg dan 60 kg. Peluru A bergerak dengan halaju  $20 \text{ ms}^{-1}$  seurus sebelum melanggar peluru B yang berada dalam keadaan pegun. Perlanggaran ini mengakibatkan peluru B melanggar peluru C yang juga dalam keadaan rehat, dan seterusnya menyebabkan peluru C bergerak ke arah dinding tegar. Jika 'pekali pengembalian' untuk perlanggaran di antara peluru A dan B ialah 0.3, dan sebanyak 0.8 bagi perlanggaran di antara peluru B dan C, tentukan:

(a) halaju peluru meriam B,  $v_B$  apabila ia melanggar peluru meriam C.  
(7 markah)

(b) halaju peluru meriam C,  $v_C$  ketika ia melanggar dinding tegar.  
(7 markah)

(c) halaju peluru meriam C,  $v_C$  apabila ia melantun dari dinding tegar jika 'pekali pengembalian' di antara keduanya adalah 0.75.  
(6 markah)

- S3** Sebuah kotak kayu diangkat dari lantai dengan menggunakan sistem tiga takal seperti dalam **RAJAH S3**. Kotak ini disambung ke takal C dengan kabel yang tidak memanjang. Pergerakan kotak, takal A, takal B dan takal C dikawal oleh kabel D yang bergerak dengan pecutan malar,  $a_D = 2 \text{ m/s}^2$  dan halaju awal,  $(V_O)_D = 4 \text{ m/s}$ , pada arah yang ditunjuk. Takal A dan takal B adalah dari jenis dwi takal. Pada masa,  $t = 10$  saat, tentukan:
- bilangan pusingan,  $N$  ppm dari takal A. (4 markah)
  - halaju sudut takal B,  $\omega_B$  rad/s. (4 markah)
  - magnitude dan arah pecutan titik E pada takal B,  $a_E \text{ m/s}^2$ . (4 markah)
  - halaju,  $v$  m/s dan jarak,  $S$  meter kotak ini bergerak. (8 markah)
- S4** (a) Bar AB pada sambungan yang ditunjuk dalam **RAJAH S4(a)** berpusing pada arah putaran jam dengan halaju sudut,  $\omega = 30 \text{ rad/s}$  apabila  $\theta = 60^\circ$ . Dengan menggunakan kaedah pusat seketika halaju sifar, tentukan halaju sudut,  $\omega$  (magnitude dan arah) anggota BC dan roda CD pada ketika ini. (5 markah)
- (b) Pada ketika yang ditunjuk dalam **RAJAH S4(b)**, sambungan AB berpusing dengan halaju sudut,  $\omega_{AB} = 2 \text{ rad/s}$  dan pecutan sudut,  $\alpha_{AB} = 6 \text{ rad/s}^2$ . Pada ketika,  $\theta = 60^\circ$ , tentukan:
- magnitud dan arah pecutan pada pin B,  $a_B \text{ m/s}^2$ . (2 markah)
  - halaju sudut sambungan BC,  $\omega_{BC}$  rad/s dan sambungan CD,  $\omega_{CD}$  rad/s. (4 markah)
  - pecutan sudut sambungan CB,  $\alpha_{CB}$  rad/s<sup>2</sup>. (5 markah)
  - pecutan sudut sambungan CD,  $\alpha_{CD}$  rad/s<sup>2</sup>. (4 markah)

**S5** Dua keluli seragam, rod langsing dan plat nipis, dikimpal bersama-sama untuk membentuk sebuah bandul seperti yang ditunjukkan dalam **RAJAH S5**. Ketumpatan bagi rod langsing  $1.5 \text{ kg/m}$  dan plat nipis  $10 \text{ kg/m}^2$ . Tentukan:

(a) jisim rod langsing dan plat nipis. (4 markah)

(b) kedudukan pusat jisim,  $G$  bagi bandul tersebut. (4 markah)

(c) momen inersia bandul tersebut pada satu paksi berserenjang kepada halaman ini dan melalui  $G$ . (6 markah)

(d) momen inersia bandul tersebut pada satu paksi berserenjang kepada halaman ini dan melalui  $O$ . (6 markah)

**S6** Sebuah spring yang mempunyai kekakuan  $k = 600 \text{ N/m}$  disambungkan ke titik  $B$  pada sebatang rod berjisim  $6 \text{ kg}$ , dengan panjang sebelum regangan adalah  $300 \text{ mm}$  seperti yang ditunjukkan dalam **Rajah S6**. Jika rod dilepaskan dari keadaan rehat pada  $\theta = 30^\circ$  hingga  $\theta = 0^\circ$ :

(a) lakarkan gambarajah rod, apabila ia berada pada kedudukan awal ( $\theta = 30^\circ$ ) dan akhir ( $\theta = 0^\circ$ ). (4 markah)

(c) hitungkan jumlah tenaga upaya pada kedudukan awal dan akhir. (8 markah)

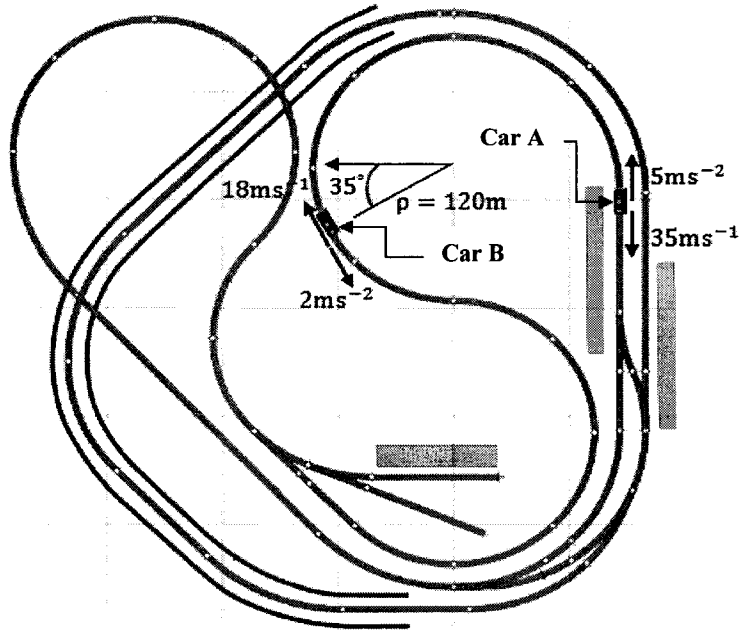
(d) tentukan halaju sudut,  $\omega$  rod pada ketika  $\theta = 0^\circ$ . (8 markah)

- END OF QUESTIONS -

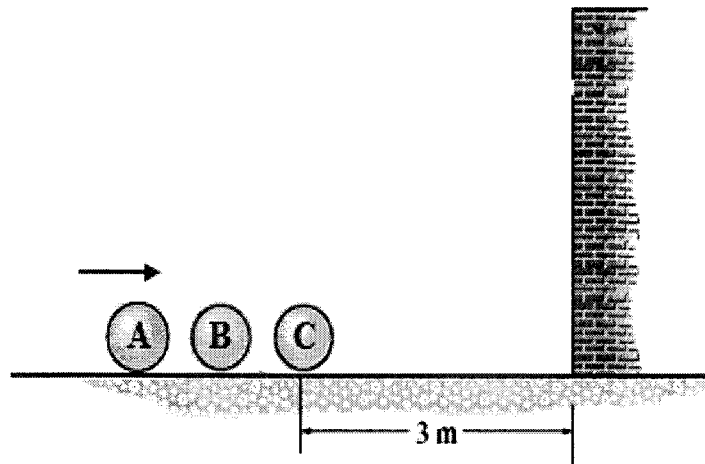
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**FIGURE Q1 / RAJAH S1**



**FIGURE Q2 / RAJAH S2**



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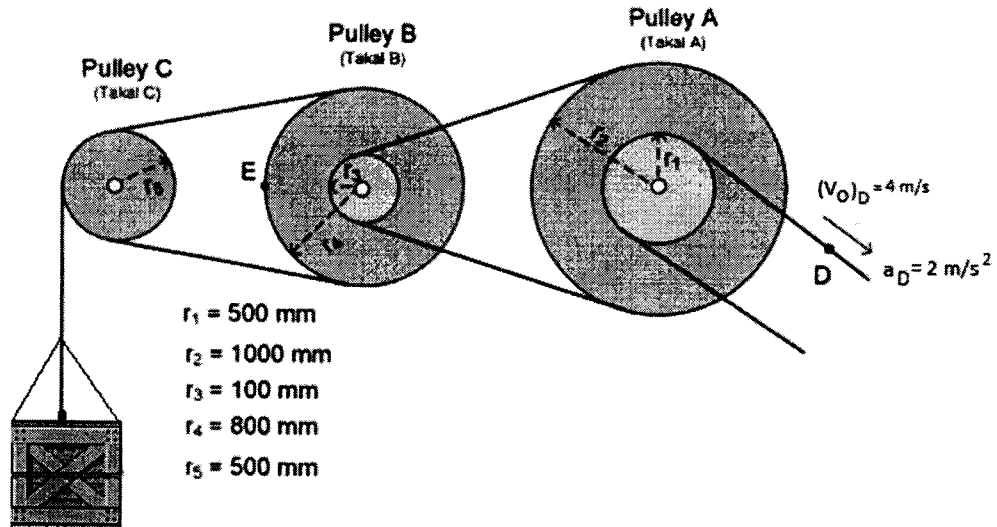


FIGURE Q3/ RAJAH S3

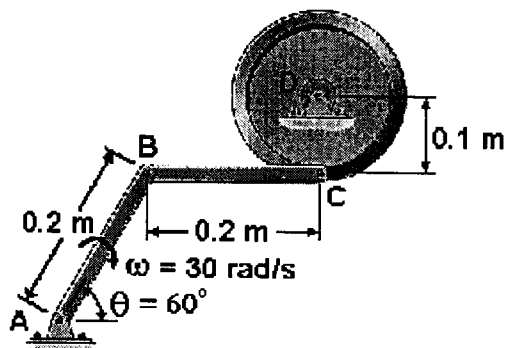


FIGURE Q4(a) / RAJAH S4(a)

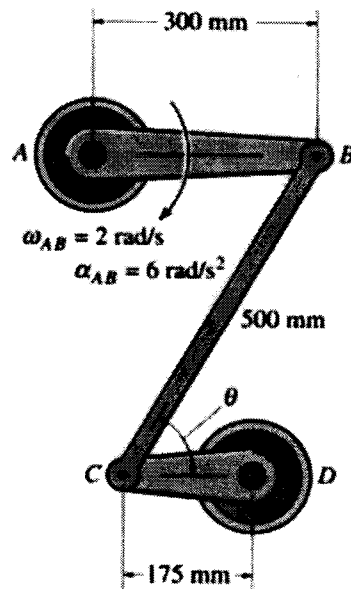
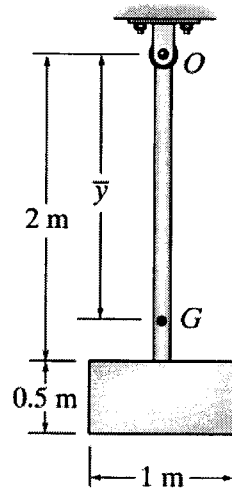


FIGURE Q4(b) / RAJAH S4(b)

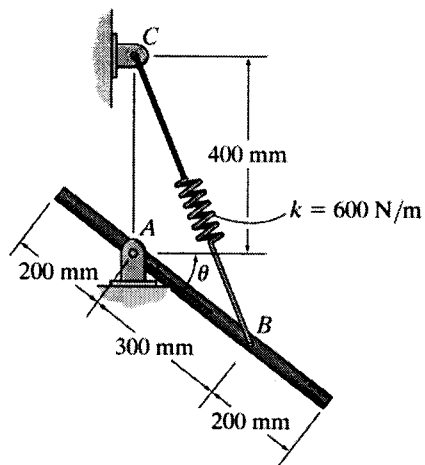
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**FIGURE Q5 / RAJAH S5**



**FIGURE Q6/ RAJAH S6**

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$$s = s_0 + v_0 t + \frac{1}{2} a t^2$$

$$v = v_0 + a t$$

$$v^2 = v_0^2 + 2 a s$$

$$\theta = \theta_0 + \omega t + \frac{1}{2} \alpha t^2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + 2 \alpha s$$

$$\mathbf{v} = \mathbf{v}^r + \mathbf{v}^\theta$$

$$\mathbf{v}^\theta = r \omega \quad \mathbf{v}^r = \dot{r}$$

$$\mathbf{a} = \mathbf{a}^r + \mathbf{a}^\theta$$

$$\mathbf{a}^r = \ddot{r} - \dot{\theta}^2 r$$

$$\mathbf{a}^\theta = \ddot{\theta} r + 2 \dot{\theta} \dot{r}$$

$$\mathbf{a} = \mathbf{a}^n + \mathbf{a}^t$$

$$\mathbf{a}^n = r \omega^2 = \frac{v^2}{r}$$

$$U = \Delta T + \Delta V_g + \Delta V_e$$

$$\Delta T = \frac{1}{2} m (v_2^2 - v_1^2) + \frac{1}{2} I_G (\omega_2^2 - \omega_1^2)$$

$$\Delta V_g = m g (h_2 - h_1)$$

$$\Delta V_e = \frac{1}{2} k (x_2^2 - x_1^2)$$

$$m v_1 + \sum \int_{t_1}^{t_2} F dt = m v_2$$

$$(H_0)_1 + \sum \int_{t_1}^{t_2} M_0 dt = (H_0)_2$$

Given formula:

$$I_{zz} = \frac{1}{12} m (a^2 + b^2) \text{ for thin plate}$$

$$I_{zz} = \frac{1}{12} m l^2 \text{ for slender rod}$$

$$m_A (v_A)_1 + m_B (v_B)_1 = m_A (v_A)_2 + m_B (v_B)_2$$

$$I_G \omega_1 + m (v_G)_1 d_1 + \sum \int M_A dt = I_G \omega_2 + m (v_G)_2 d_2$$

$$e = - \frac{(v_B)_2^n - (v_A)_2^n}{(v_B)_1^n - (v_A)_1^n}$$

$$(v_A)_1^t = (v_A)_2^t$$

$$\sum M_G = I_G \alpha$$

$$\sum F = m a$$

$$T_1 + V_1 = T_2 + V_2$$

$$\mathbf{v}_P = \mathbf{v}_{P'} + \mathbf{v}_{P/Oxy}$$

$$\mathbf{v}_P = (\ddot{\mathbf{r}})_{Oxy} = \boldsymbol{\Omega} \times \mathbf{r} + (\dot{\mathbf{r}})_{Oxy}$$

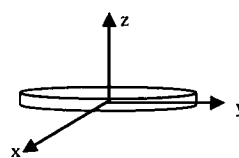
$$\mathbf{a}_P = \mathbf{a}_{P'} + \mathbf{a}_{P/Oxy} + \mathbf{a}_C$$

$$\mathbf{a}_P = \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{r}) + \dot{\boldsymbol{\Omega}} \times \mathbf{r} + 2(\boldsymbol{\Omega} \times (\dot{\mathbf{r}})_{Oxy}) + (\ddot{\mathbf{r}})_{Oxy}$$

$$I = m k_G^2$$

$$I_{xx} = I_{yy} = \frac{1}{4} m r^2$$

$$I_{zz} = \frac{1}{2} m r^2$$



$$I_{xx} = I_{yy} = \frac{1}{12} m l^2$$

$$I_{x'x'} = \frac{1}{3} m l^2$$

