



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER I  
SESSION 2019/2020**

COURSE NAME : SIGNALS AND SYSTEMS  
COURSE CODE : BNF 36002  
PROGRAMME CODE : BNF  
EXAMINATION DATE : DECEMBER 2019 / JANUARY 2020  
DURATION : 2 HOURS  
INSTRUCTION : ANSWER ALL QUESTIONS

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THIS QUESTION PAPER CONSISTS OF **NINE (9)** PAGES

**Q1** (a) Briefly explain continuous-time and discrete-time signals and systems with the aid of graphical representations and block diagrams.

(6 marks)

(b) The signal  $x(t) = \cos(\pi t/4) + \sin(\pi t/8)$  consists of two continuous-time periodic signal. Determine the period  $T$  of the signal.

(7 marks)

(c) Write the signal  $x(t)$  for **Figure Q1(c)** using a single analytical expression with aid of the unit step function,  $u(t)$ .

(7 marks)

**Q2** (a) Explain the differences between causality and invertible system

(4 marks)

(b) Consider a periodic signal  $x(t)$  is defined by

$$x(t) = 3 + 4 \sin(2\omega_0 t) + 7 \cos(4\omega_0 t + 30^\circ)$$

(i) Determine exponential Fourier Series coefficient of signal  $x(t)$ .

(7 marks)

(ii) Sketch the magnitude and phase spectrum of signal  $x(t)$ .

(2 marks)

(c) Compute the coefficients  $a_k$  using Fourier series analysis equation for the continuous-time periodic signal

$$x(t) = \begin{cases} 1.5 & 0 \leq t < 1 \\ -1.5 & 1 \leq t < 2 \end{cases}$$

with the fundamental frequency  $\omega_0 = \pi$

$$\text{Fourier series analysis equation } a_k = \frac{1}{T} \int_T x(t) e^{-jk\omega_0 t} dt$$

(7 marks)

**Q3** (a) Briefly explain how Fourier Transform (FT) is obtained from Fourier series and the convolution property of FT.

(4 marks)

(b) Determine the Fourier Transform of following signals using the definition of FT.

(i)  $x(t) = 2e^{-\frac{t}{5}} u(t - 2)$

(8 marks)

(ii)  $x(t) = \sin(2\pi t) + \cos(4\pi t)$

(8 marks)



- Q4** (a) Using the definition of Laplace transform, determine the Laplace transform of  $x(t) = 3e^{-3t}u(t - 2)$ .  
(5 marks)
- (b) Sketch the zero-pole plot and region of convergence (if exist) of the signal  $x(t)$  from **Q4(a)**.  
(3 marks)
- (c) A Linear Time Invariant (LTI) system is shown in **Figure Q4(c)** has an impulse response  $h(t) = 0.25e^{-3t}u(t)$ . If the system produces output  $y(t) = (e^{-t} - e^{-2t})u(t)$ , determine the input  $x(t)$ .  
(12 marks)

- END OF QUESTIONS -

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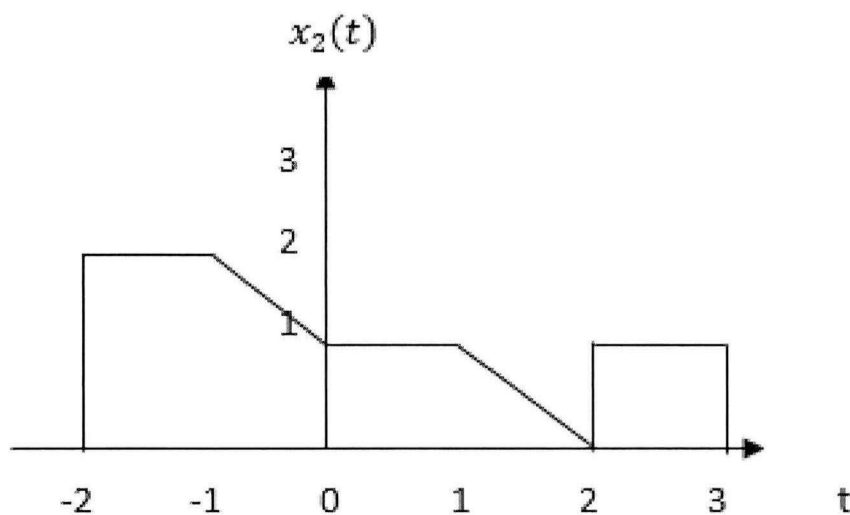


Figure Q1(c)

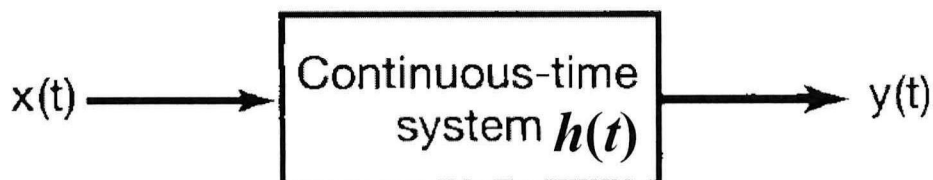


Figure Q4(c)

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**TABLE 1: INDEFINITE INTEGRALS**

$\int \cos at \, dt = \frac{1}{a} \sin at$	$\int \sin at \, dt = -\frac{1}{a} \cos at$
$\int t \cos at \, dt = \frac{1}{a^2} \cos at + \frac{1}{a} t \sin at$	$\int t \sin at \, dt = \frac{1}{a^2} \sin at - \frac{1}{a} t \cos at$

**TABLE 2: EULER'S IDENTITY**

$e^{\pm j\frac{\pi}{2}} = \pm j$	$A \angle \pm \theta = Ae^{\pm j\theta}$
$e^{\pm jn\pi} = \cos(n\pi)$	$e^{\pm j\theta} = \cos \theta \pm j \sin \theta$
$\cos \theta = \frac{1}{2}(e^{j\theta} + e^{-j\theta})$	$\sin \theta = \frac{1}{2}(e^{j\theta} - e^{-j\theta})$

**TABLE 3: TRIGONOMETRIC IDENTITIES**

$\sin \alpha = \cos \left( \alpha - \frac{\pi}{2} \right)$	$\cos \alpha = \sin \left( \alpha + \frac{\pi}{2} \right)$
$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$	$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$
$\sin 2\alpha = 2 \sin \alpha \cos \alpha$	$\cos 2\alpha = 2 \cos^2 \alpha - 1$
$\cos 2\alpha = 1 - 2 \sin^2 \alpha$	$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$

**TABLE 4: VALUES OF COSINE, SINE AND EXPONENTIAL FUNCTIONS FOR INTEGRAL MULTIPLE OF  $\pi$**

Function	Value	Function	Value
$\cos(2n\pi)$	1	$e^{\frac{jn\pi}{2}}$	$\begin{cases} (-1)^{\frac{n}{2}} & , n = \text{even} \\ (-1)^{\frac{n-1}{2}} & , n = \text{odd} \end{cases}$
$\sin(2n\pi)$	0		
$\cos(n\pi)$	$(-1)^n$	$\cos\left(\frac{n\pi}{2}\right)$	$\begin{cases} (-1)^{\frac{n}{2}} & , n = \text{even} \\ 0 & , n = \text{odd} \end{cases}$
$\sin(n\pi)$	0		
$e^{j2n\pi}$	1	$\sin\left(\frac{n\pi}{2}\right)$	$\begin{cases} (-1)^{\frac{n-1}{2}} & , n = \text{even} \\ (-1)^{\frac{n+1}{2}} & , n = \text{odd} \end{cases}$
$e^{jn\pi}$	$(-1)^n$		

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**TABLE 6: FOURIER TRANSFORM PAIRS**

Time domain, $x(t)$	Frequency domain, $X(\omega)$	Time domain, $x(t)$	Frequency domain, $X(\omega)$
$\delta(t)$	1	$t^n e^{-at} u(t)$	$\frac{n!}{(a + j\omega)^{n+1}}$
1	$2\pi\delta(\omega)$	$e^{-a t }$	$\frac{2a}{a^2 + \omega^2}$
$u(t)$	$\pi\delta(\omega) + \frac{1}{j\omega}$	$e^{-j\omega_0 t}$	$2\pi\delta(\omega - \omega_0)$
$u(t - \tau) - u(t + \tau)$	$2 \frac{\sin \omega\tau}{\omega}$	$\sin \omega_0 t$	$j\pi[\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$
$ t $	$\frac{-2}{\omega^2}$	$\cos \omega_0 t$	$\pi[\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$
$\text{sgn}(t)$	$\frac{2}{j\omega}$	$e^{-at} \sin \omega_0 t u(t)$	$\frac{\omega_0}{(a + j\omega)^2 + \omega_0^2}$
$e^{-at} u(t)$	$\frac{1}{a + j\omega}$	$e^{-at} \cos \omega_0 t u(t)$	$\frac{a + j\omega}{(a + j\omega)^2 + \omega_0^2}$
$e^{at} u(-t)$	$\frac{1}{\alpha - j\omega}$		

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**TABLE 8: LAPLACE TRANSFORM**

$x(t), t > 0$	$X(s)$	$x(t), t > 0$	$X(s)$
$\delta(t)$	1	$\cos bt$	$\frac{s}{s^2 + b^2}$
$u(t)$	$\frac{1}{s}$	$\sin bt$	$\frac{b}{s^2 + b^2}$
$t$	$\frac{1}{s^2}$	$e^{-at} \cos bt$	$\frac{s + a}{(s + a)^2 + b^2}$
$t^n$	$\frac{n!}{s^{n+1}}$	$e^{-at} \sin bt$	$\frac{b}{(s + a)^2 + b^2}$
$e^{-at}$	$\frac{1}{s + a}$	$t \cos bt$	$\frac{s^2 - b^2}{(s^2 + b^2)^2}$
$te^{-at}$	$\frac{1}{(s + a)^2}$	$t \sin bt$	$\frac{2bs}{(s^2 + b^2)^2}$

**TABLE 9: LAPLACE TRANSFORM PROPERTIES**

Name	Operation in Time Domain	Operation in Frequency Domain
1. Linearity	$a_1x_1(t) + a_2x_2(t)$	$a_1X_1(s) + a_2X_2(s)$
2. Differentiation	$\frac{d^n x(t)}{dt^n}$	$s^n X(s) - s^{n-1}x(0^-) - \dots - x^{(n-1)}(0^-)$
3. Integration	$\int_{-\infty}^t x(\lambda) d\lambda$	$\frac{X(s)}{s} + \frac{x^{(-1)}(0^-)}{s}$
4. s-shift	$x(t) \exp(-\alpha t)$	$X(s + \alpha)$
5. Delay	$x(t - t_0)u(t - t_0)$	$X(s) \exp(-st_0)$
6. Convolution	$x_1(t) * x_2(t) = \int_0^{\infty} x_1(\lambda)x_2(t - \lambda) d\lambda$	$X_1(s)X_2(s)$
7. Product	$x_1(t)x_2(t)$	$\frac{1}{2\pi j} \int_{c-j\infty}^{c+j\infty} X_1(s - \lambda)X_2(\lambda) d\lambda$
8. Initial value (provided limits exist)	$\lim_{t \rightarrow 0^+} x(t)$	$\lim_{s \rightarrow \infty} sX(s)$
9. Final value (provided limits exist)	$\lim_{t \rightarrow \infty} x(t)$	$\lim_{s \rightarrow 0} sX(s)$
10. Time scaling	$x(at), a > 0$	$a^{-1}X\left(\frac{s}{a}\right)$

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