



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER I  
SESSION 2016/2017**

COURSE NAME : CONTROL SYSTEM THEORY  
COURSE CODE : BEH 30603  
PROGRAMME CODE : BEJ  
EXAMINATION DATE : DECEMBER 2016/JANUARY 2017  
DURATION : 3 HOURS  
INSTRUCTION : ANSWER ALL QUESTIONS

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DR. MOHD NOR HAZIM CHOWDHURY  
Professor of Control Systems & Robotics  
Faculty of Engineering & Technology  
Universiti Tun Hussein Onn Malaysia  
THIS QUESTION PAPER CONSISTS OF FIVE (5) PAGES ONLY

- Q1** (a) Draw the general block diagram for the closed loop control system. (4 marks)
- (b) Differentiate clearly the function of each component in the block diagram that you have drawn in question **Q1(a)**. (10 marks)
- (c) By using a practical example, analyse the effect of disturbance on a closed loop control system. (6 marks)

**Q2** **Figure Q2** shows a block diagram of a position control system which employs velocity feedback. The amplifier gain and tachometer constant for this control system are given by  $K_s$  and  $K_g$  respectively.

- (a) Formulate the transfer function  $C(s)/R(s)$ . (4 marks)
- (b) Select suitable values for  $K_s$  and  $K_g$  so that the output response for a unit step input, will have a maximum overshoot of 9.47% at time  $t = 0.3927$  second. (8 marks)
- (c) By using these selected values for  $K_s$  and  $K_g$ , derive the unit step response  $c(t)$  of the system. (8 marks)

- Q3** (a) Define the term *root locus* which applies to control system. (2 marks)
- (b) Consider a control system with unity feedback which has the open-loop transfer function:

$$G(s) = \frac{K}{(s+4)^3}$$

- (i) By using Routh-Hurwitz stability criteria, investigate the values of  $K$  for this control system to be stable. (4 marks)
- (ii) Produce the root locus for this control system based on the procedure for sketching root locus. (10 marks)

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- (iii) Select a suitable value for  $K$  from the root locus, so that the unit step response of this control system will be under damped.

(4 marks)

- Q4** (a) Investigate the phenomenon that will occur in a control system when an on-off controller is being employed in the system.

(5 marks)

- (b) Analyse the requirement of a dead-zone or neutral zone in an on-off controller.

(5 marks)

- (c) The temperature of water in a tank is controlled by an on-off controller. When the heater is *off* the temperature drops at  $2^\circ\text{C}$  per minute. When the heater is *on* the temperature rises at  $4^\circ\text{C}$  per minute. The setpoint or the input is  $50^\circ\text{C}$  and the neutral zone is  $\pm 20\%$  of the setpoint. There is a  $0.5$  min lag at the *on* and *off* switch points.

- (i) Plot the water temperature versus time.

(7 marks)

- (ii) Determine the period of oscillation.

(3 marks)

- Q5** A single input single output control system can be represented by the state equation and output equation respectively as  $\dot{\underline{x}}(t) = A\underline{x}(t) + B\underline{u}(t)$  and  $y(t) = C\underline{x}(t)$ , where the matrices  $A$ ,  $B$  and  $C$  are given respectively by:

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \text{ and } C = [1 \quad 0]$$

- (a) Write down an expression for the transformed states  $X(s)$ .

(3 marks)

- (b) Formulate the state transition matrix  $\Phi(t)$  for this system.

(10 marks)

- (c) Formulate the output  $y(t)$  when the system is subjected to a unit step input and the initial states are given by  $\underline{x}(0) = [0 \quad 0]^T$ .

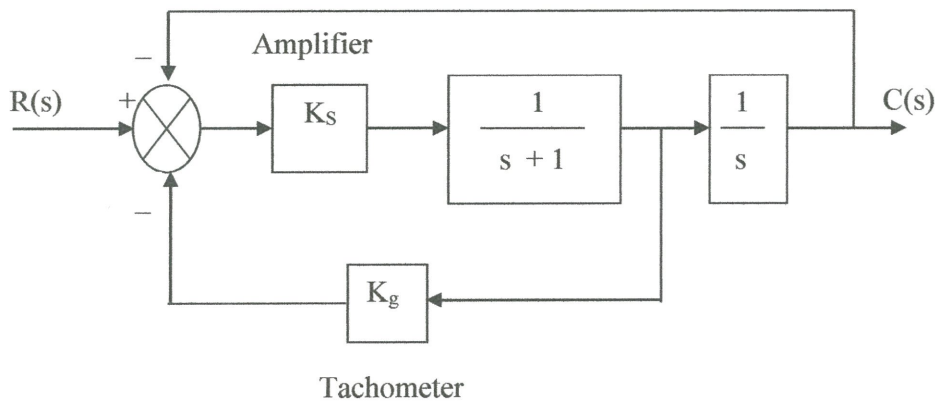
(7 marks)

– END OF QUESTIONS –

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**FIGURE Q2**

**Table 1** : Laplace Transform Table

$f(t)$	$F(s)$
$u(t)$	$\frac{1}{s}$
$e^{-at}u(t)$	$\frac{1}{s+a}$
$\sin \omega t u(t)$	$\frac{\omega}{s^2 + \omega^2}$
$\cos \omega t u(t)$	$\frac{s}{s^2 + \omega^2}$
$e^{-at} \sin \omega t u(t)$	$\frac{\omega}{(s+a)^2 + \omega^2}$
$e^{-at} \cos \omega t u(t)$	$\frac{s+a}{(s+a)^2 + \omega^2}$

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**Table 2** : Second order prototype equations

$\frac{C(s)}{R(s)} = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$	$T_r = \frac{\pi - \cos^{-1} \zeta}{\omega_n \sqrt{1 - \zeta^2}}$
$\mu_p = e^{\frac{-\zeta\pi}{\sqrt{1 - \zeta^2}}}$	$T_p = \frac{\pi}{\omega_n \sqrt{1 - \zeta^2}}$
$T_s = \frac{4}{\zeta\omega_n} \text{ (2\% criterion)}$	$T_s = \frac{3}{\zeta\omega_n} \text{ (5\% criterion)}$

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