



UNIVERSITI TUN HUSSEIN ONN MALAYSIA

FINAL EXAMINATION

SEMESTER I

SESSION 2015/2016

COURSE NAME	:	CONTROL SYSTEM THEORY
COURSE CODE	:	BEH30603
PROGRAMME	:	BACHELOR OF ELECTRONIC ENGINEERING WITH HONOURS
EXAMINATION DATE	:	DECEMBER 2015/JANUARY 2016
DURATION	:	3 HOURS
INSTRUCTION	:	ANSWER ALL QUESTIONS

THIS QUESTION PAPER CONSISTS OF FOUR (4) PAGES ONLY

- Q1** (a) Describe the conditions for a point to be on the root locus. (3 marks)
- (b) By using the general rules for sketching root locus, sketch the root locus for a control system with the following transfer functions:

$$G(s) = \frac{K}{(s-1)(s^2+4s+7)} \quad \text{and } H(s) = 1$$

(13 marks)

- (c) Select the value of the gain K such that the dominant closed-loop poles will have a damping ratio of 0.5. (4 marks)

- Q2** (a) Explain how the Bode diagram can be used to determine the absolute stability of a closed-loop control system. (4 marks)
- (b) By using the asymptotic or straight line approximation method, draw the Bode diagram for a control system with the open loop transfer function is given by:

$$G(s)H(s) = \frac{10}{s(s+1)(s+10)}$$

(12 marks)

- (c) Analyze the stability of this control system. (4 marks)

- Q3** (a) Explain the function of a compensator in control system. (4 marks)
- (b) **Figure Q3(b)** shows a phase lag compensator circuit. Formulate the transfer function of $E_o(s)/E_i(s)$ where $E_o(s)$ and $E_i(s)$ are the Laplace transformation of $e_o(t)$ and $e_i(t)$ respectively. (6 marks)
- (c) Design a phase lag compensator circuit for a control system in such a way that the steady state error can be reduced by 10 times for a unit step input and the open loop transfer function of the control system with unity feedback is given by:

$$G(s) = \frac{165}{(s+1)(s+2)(s+10)}$$

(10 marks)

- Q4** A single input single output control system can be represented by the state equation and output equation respectively as $\dot{\underline{x}} = A\underline{x}(t) + B\underline{u}(t)$ and $y(t) = C\underline{x}(t)$, where the matrices A, B and C are given respectively by:

$$A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad \text{and} \quad C = [1 \quad 0]$$

- (a) Determine the state transition matrix $\Phi(t)$ for this system. (10 marks)
- (b) Obtain the output $y(t)$ when the system is subjected to a unit step input and the initial states are given by $\underline{x}(0) = [0 \quad 0]^T$. (10 marks)

- Q5** The state equation of a single input single output control system can be represented by the equation $\dot{\underline{x}} = A\underline{x}(t) + B\underline{u}(t)$ where the matrices A and B are given respectively by:

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -6 & -5 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

- (a) Calculate the eigenvalues for this system. (5 marks)
- (b) Analyze the controllability of this control system. (5 marks)
- (c) This control system is to be compensated by state variable feedback where the specified eigenvalues are $s = -2 \pm j4$, and $s = -10$. Design the closed-loop control system by specifying the gains in the feedback paths. (10 marks)

– END OF QUESTION –

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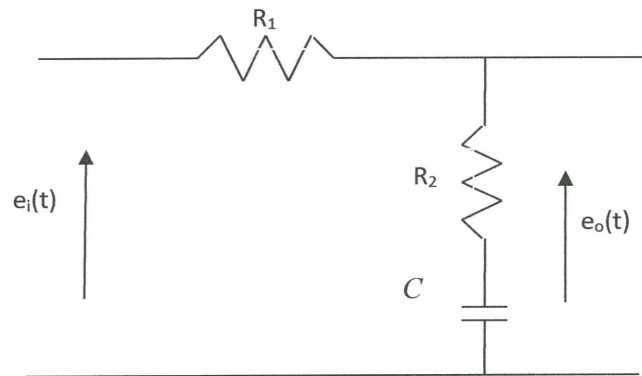


FIGURE Q3(b)

TABLE 1 : Laplace Transform Table

$f(t)$	$F(s)$
$u(t)$	$\frac{1}{s}$
$e^{-at}u(t)$	$\frac{1}{s+a}$
$e^{-at} \sin \omega t u(t)$	$\frac{\omega}{(s+a)^2 + \omega^2}$
$e^{-at} \cos \omega t u(t)$	$\frac{s+a}{(s+a)^2 + \omega^2}$