



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER I  
SESSION 2012/2013**

COURSE NAME : CONTROL SYSTEM THEORY /  
CONTROL SYSTEM

COURSE CODE : BEH 30603 / BEE 3143

PROGRAMME : BEH / BEE

EXAMINATION DATE : JANUARY 2013

DURATION : 2 HOURS 30 MINUTES

INSTRUCTION : ANSWER **FOUR (4)** QUESTIONS  
ONLY

THIS QUESTION PAPER CONSISTS OF NINE (9) PAGES

- Q1. (a)** Explain the following concisely
- (i) Control system (3 marks)
  - (ii) Block diagram (3 marks)
  - (iii) Time-invariant (3 marks)
  - (iv) Process control (3 marks)
- (b) Give an example of a real practical application for a closed loop control system. Identify the input and output variables and by using a suitable block diagram, describe the operation of the selected application. (13 marks)

- Q2.** Figure Q2 shows an armature-controlled d.c. motor with non zero armature inductance. This motor is assumed to have a constant magnetic field. The parameters for this motor are defined as follows:

$k_b$  = back e.m.f. constant,

$k_t$  = motor torque constant,

$J_m$  = moment of inertia of the motor and load referred to the motor shaft,

$B_m$  = viscous friction constant of the motor and load referred to the motor shaft.

Draw the block diagram of the armature-controlled d.c motor and derive its transfer function  $\theta_m(s)/V_a(s)$  where  $\theta_m(s)$  and  $V_a(s)$  are the Laplace transform of the angular displacement  $\theta_m(t)$  and the motor voltage  $V_a(t)$  respectively.

(25 marks)

**Q3** (a) Name and sketch the three responses for a second order system. (6 marks)

(b) A control system is shown in Figure Q3. If the reference input  $r(t)$  is a unit step function, derive the expression for its output response  $c(t)$ . Hence determine:

- i. The rise time  $t_r$ .
- ii. The peak-time  $t_p$ .
- iii. The maximum overshoot and percentage overshoot.

Sketch the output response  $c(t)$ . (19 marks)

**Q4** By using the general rules for sketching a root locus, sketch the root locus for a control system as shown in Figure Q4. (16 marks)

From the root locus

- (a) Determine the range of  $K$  so that the system response will be over-damped. (3 marks)
- (b) Obtain the value of  $K$  so that the response is critically damped. (3 marks)
- (c) Determine the range of  $K$  so that the response is under-damped (3 marks)

**Q5.** The open-loop transfer function of a unity feedback control system is given by

$$G(s) = \frac{5}{s(s+2)}.$$

Design a lead compensator which gives  $\omega_n = 4$  rad/sec and  $\zeta = 0.5$ .

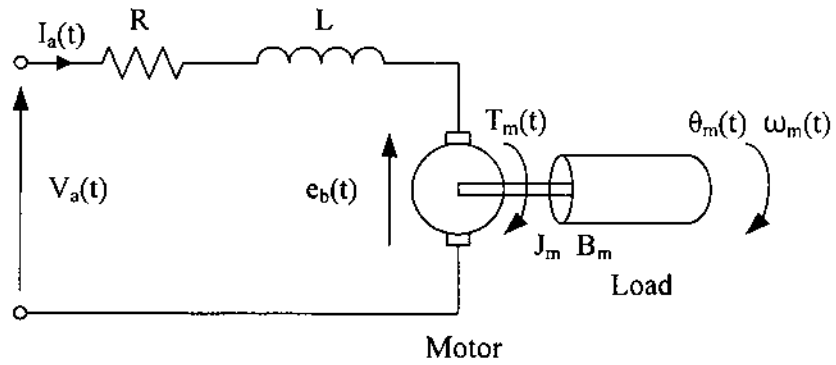
- (a) Obtain the closed-loop transfer function and the poles of the uncompensated system. (4 marks)
- (b) Obtain the desired poles if the lead compensator has been added. (2 marks)
- (c) Obtain the angle of the compensator in the desired pole. (5 marks)
- (d) Obtain the poles and zeros of the compensator. (9 marks)
- (e) Obtain the gain of the compensator and hence give the transfer function of the compensator (5 marks)

**-END OF QUESTION-**

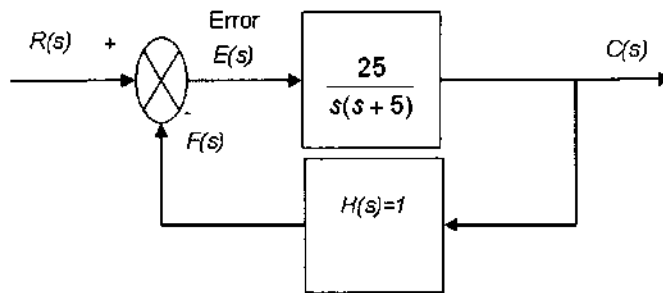
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**FIGURE Q2**

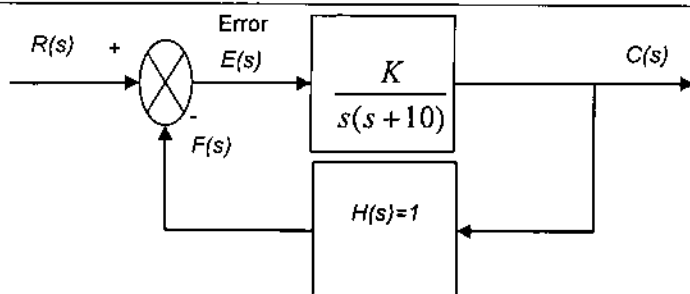


**FIGURE Q3**

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**FIGURE Q4**

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Table 1: Laplace transform table

$f(t)$	$F(s)$
$\delta(t)$	1
$u(t)$	$\frac{1}{s}$
$tu(t)$	$\frac{1}{s^2}$
$t^n u(t)$	$\frac{n!}{s^{n+1}}$
$e^{-at}u(t)$	$\frac{1}{s+a}$
$\sin \omega t u(t)$	$\frac{\omega}{s^2 + \omega^2}$
$\cos \omega t u(t)$	$\frac{s}{s^2 + \omega^2}$
$e^{-at} \sin \omega t u(t)$	$\frac{\omega}{(s+a)^2 + \omega^2}$
$e^{-at} \cos \omega t u(t)$	$\frac{s+a}{(s+a)^2 + \omega^2}$

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**Table 2: Laplace transform theorems**

Name	Theorem
Frequency shift	$\mathcal{L}[e^{-at} f(t)] = F(s + a)$
Time shift	$\mathcal{L}[f(t - T)] = e^{-sT} F(s)$
Differentiation	$\mathcal{L}\left[\frac{d^n f}{dt^n}\right] = s^n F(s) - \sum_{k=1}^n s^{n-k} f^{(k-1)}(0^-)$
Integration	$\mathcal{L}\left[\int_0^t f(\tau) d\tau\right] = \frac{F(s)}{s}$
Initial value	$\lim_{t \rightarrow 0} f(t) = \lim_{s \rightarrow \infty} sF(s)$
Final value	$\lim_{t \rightarrow \infty} f(t) = \lim_{s \rightarrow 0} sF(s)$



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**Table 3: 2<sup>nd</sup> Order prototype system equations**

$\frac{C(s)}{R(s)} = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$	$T_r = \frac{\pi - \cos^{-1} \zeta}{\omega_n \sqrt{1 - \zeta^2}}$
$\mu_p = e^{\frac{-\zeta\pi}{\sqrt{1 - \zeta^2}}}$	$T_p = \frac{\pi}{\omega_n \sqrt{1 - \zeta^2}}$
$T_s = \frac{4}{\zeta\omega_n} \text{ (2\% criterion)}$	$T_s = \frac{3}{\zeta\omega_n} \text{ (5\% criterion)}$