



UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
SEMESTER I
SESSION 2012/2013**

COURSE NAME : TRANSFORM CIRCUIT ANALYSIS
COURSE CODE : BEF 22803
PROGRAMME : BEF
EXAMINATION DATE : JANUARY 2013
DURATION : 2 HOURS 30 MINUTES
INSTRUCTION : ANSWER **FIVE (5)** QUESTIONS ONLY

THIS QUESTION PAPER CONSISTS OF **NINE (9)** PAGES

Q1

$$f(t) = \begin{cases} 4 & \text{if } 0 < t < \pi \\ 0 & \text{if } \pi < t < 2\pi \\ 3 \sin t & \text{if } t > 2\pi \end{cases}$$

- (a) Given a piecewise function of $f(t)$
- (i) Define the function of $f(t)$
 - (ii) Sketch the function of $f(t)$
 - (iii) Formulate the Laplace Transform of $F(s)$
- (6 marks)
- (b) Explain the relationships between unit step and unit impulse function with the help of diagram.
- (6 marks)
- (c) Figure Q1(c) shows the impulse response $h(t)$ and input signal $u(t)$. Calculate the convolution of the two signals $h(t)$ and $u(t)$.
- (8 marks)

Q2

- (a) Solve the Laplace transform for the function $h(t)$ given below.

$$h(t) = 2 \int_0^t (t - \tau) e^{2\tau} d\tau$$

(5 marks)

- (b) In a circuit of Figure Q2(b), switch S is kept open for a long time and its closed at $t=0$.
- (i) Transform the circuit to Laplace transform circuit.
 - (ii) Find $i_1(t)$ and $i_2(t)$ for $t \geq 0$.
 - (iii) Formulate the voltage across 6Ω resistor $v_6(t)$.

(15 marks)

- Q3** (a) Find the solution of the initial value problem given below.

$$y''+4y = g(t), \quad y(0) = 3 \quad y'(0) = -1$$

(5 marks)

- (b) Figure Q3(b) shows the inductor of 2 henrys, resistor of 16Ω and a capacitor of 0.02 farads are connected in series with an e.m.f of E volts. At $t=0$ the charge on the capacitor and current in the circuit are zero. If $E=300$ volts, calculate,

(i) the charge, Q and

(ii) current, I

at any time $t>0$.

(15 marks)

- Q4** (a) In the circuit of Figure Q4(a), switch S_1 closes at $t=0$, while at the same time same time, switch S_2 opens. Given that $v_c(0^+) = 3V$.

(i) Sketch the s-domain equivalent circuit.

(ii) By using Laplace transform method, calculate $V_{out}(t)$ for $t>0$

(10 marks)

- (b) Figure Q4(b) shows the circuit consist of R_1 and R_2 which value are 20Ω and 80Ω respectively. The value of capacitor is 0.125 F.

(i) Evaluate the Fourier transform of $v_i(t)$.

(ii) Calculate the value of $v_o(t)$.

(10 marks)

- Q5** (a) Figure Q5(a) shows the periodic signal $f(t)$.
- (i) Formulate the Fourier series for the periodic function
 - (ii) Sketch the amplitude and phase spectra.
- (10 marks)
- (b) The circuit shown in Figure Q5(b) is supplied by the voltage source of $v_s(t) = 12e^{-2t}$ V. Calculate,
- (i) the energy delivered by the source voltage
 - (ii) the energy dissipated by 4Ω resistance.
 - (iii) the percentage of source energy transferred to the load.
 - (iv) the percentage of the energy content in 4Ω resistor if the frequency $v_o(t)$ is between $0 \leq \omega \leq 2$ rad/s
- (10 marks)

-END OF QUESTIONS-

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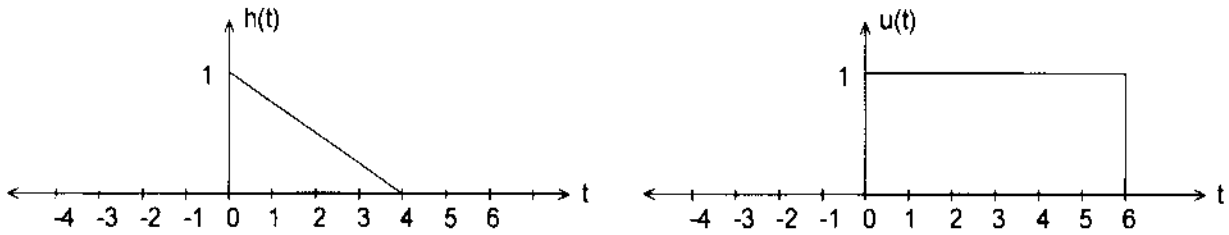


FIGURE Q1(c)

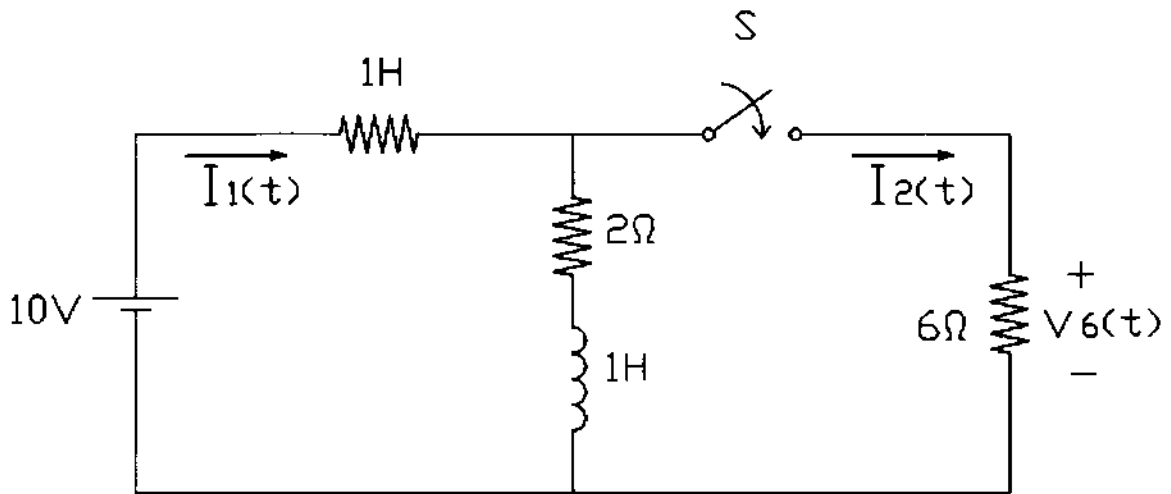


FIGURE Q2(b)

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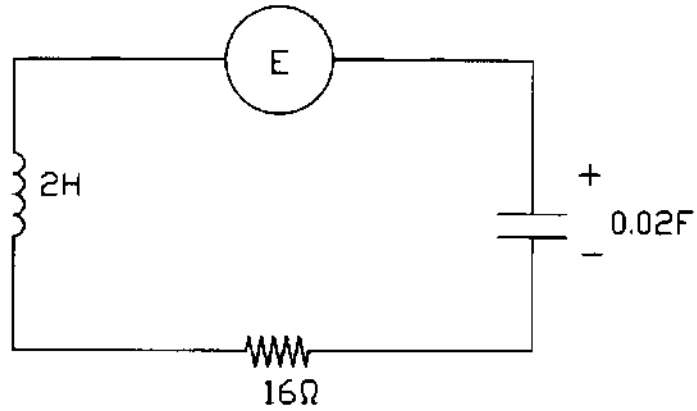


FIGURE Q3(b)

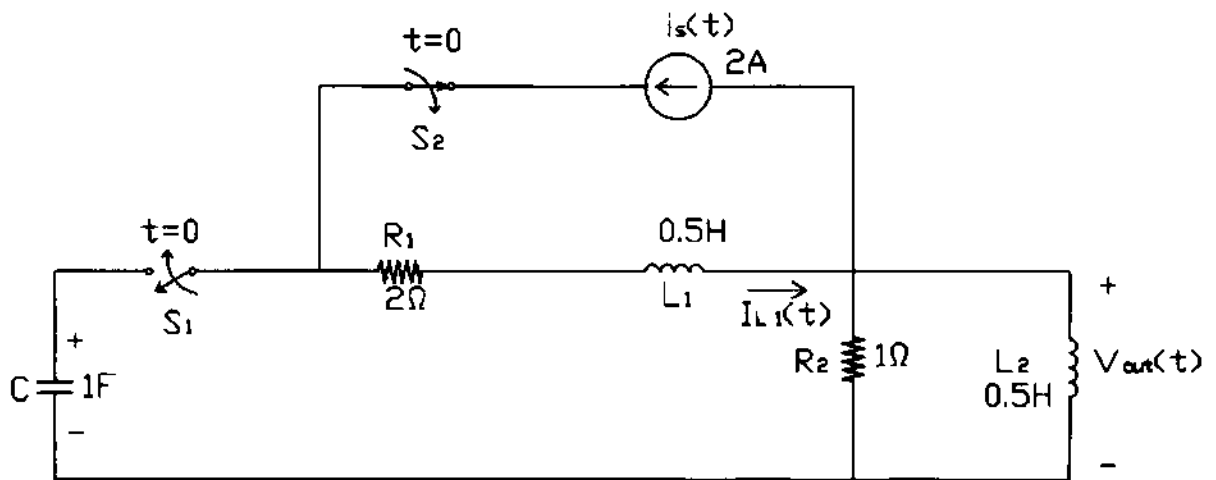
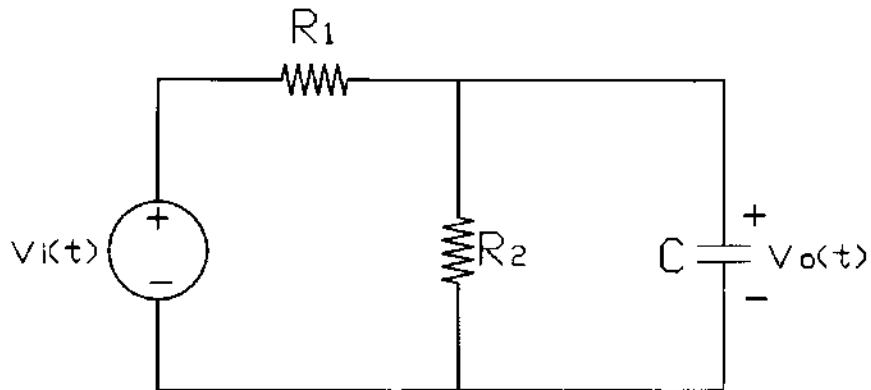
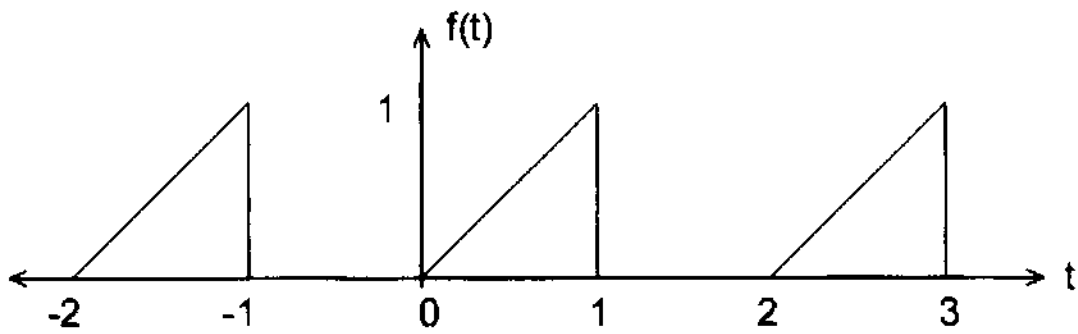


FIGURE Q4(a)

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**FIGURE Q4(b)****FIGURE Q5(a)**

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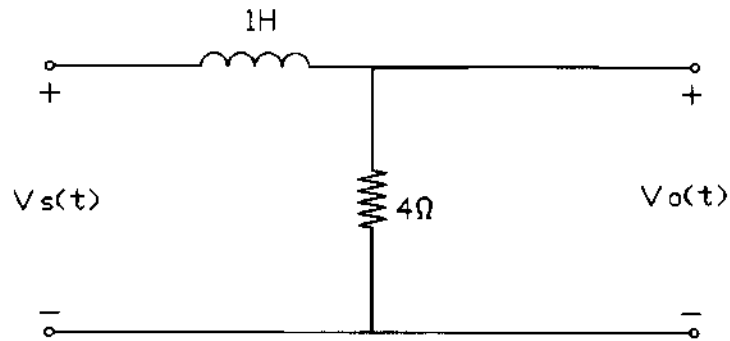


FIGURE Q5(b)

Laplace Transform Table

	$f(t)$	$F(s)$	
1	1	$\frac{1}{s}$	$s > 0$
2	t	$\frac{1}{s^2}$	$s > 0$
3	$t^n, n=1,2,\dots$	$\frac{n!}{s^{n+1}}$	$s > 0$
4	e^{at}	$\frac{1}{s-a}$	$s > a$
5	$\sin at$	$\frac{a}{s^2 + a^2}$	$s > 0$
6	$\cos at$	$\frac{s}{s^2 + a^2}$	$s > 0$
7	$\sinh at$	$\frac{a}{s^2 - a^2}$	$s > a $
8	$\cosh at$	$\frac{s}{s^2 - a^2}$	$s > a $
9	$e^{at} \sin bt$	$\frac{b}{(s-a)^2 + b^2}$	$s > a$

10	$e^{at} \cos bt$	$\frac{s-a}{(s-a)^2 + b^2}$	$s > a$
11	$t^n e^{at}$	$\frac{n!}{(s-a)^{n+1}}$	$s > a$
12	$t \sin at$	$\frac{2as}{(s^2 - a^2)^2}$	$s > 0$
13	$t \cos at$	$\frac{s^2 - a^2}{(s^2 + a^2)^2}$	$s > 0$
14	$t \sinh at$	$\frac{2as}{(s^2 - a^2)^2}$	$s > a $
15	$t \cosh at$	$\frac{s^2 + a^2}{(s^2 + a^2)^2}$	$s > a $
16	$y'(t)$	$sY(s) - y(0)$, and $Y(s) = L\{y(t)\}$	
17	$y''(t)$	$s^2Y(s) - sy(0) - y'(0)$	
18	$e^{at} f(t)$	$F(s-a)$	
19	$t^n f(t), n=1,2,\dots$	$(-1)^n \frac{d^n}{ds^n} F(s)$	
20	$\mu_a(t)f(t)$	$e^{-as} L\{f(t+a)\}$	
21	$\mu_a(t)f(t+a)$	$e^{-as} L\{f(t)\}$	
22	$f(t)$	$\frac{\int_0^{\infty} e^{-st} f(t) dt}{1 - e^{-sa}}$	
23	$\int_0^t f(\tau)g(t-\tau)d\tau$	$F(s)G(s)$	
24	$\int_0^t f(\tau)d\tau$	$\frac{1}{s} F(s)$	