

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

FINAL EXAMINATION SEMESTER I SESSION 2010/2011

COURSE NAME : ELECTRIC NETWORK ANALYSIS AND SYNTHESIS

COURSE CODE : BEE 3113 / BEX 31303

PROGRAMME : 2 BEE / 3 BEE

EXAMINATION DATE : NOVEMBER / DECEMBER 2010

DURATION : 2 HOURS 30 MINUTES

INSTRUCTION : THIS EXAMINATION PAPER CONSISTS OF PART A AND PART B. ANSWER ONLY FOUR (4) QUESTIONS FROM PART A & ONE (1) QUESTION FROM PART B.

THIS PAPER CONSISTS OF NINE (9) PAGES

PART A: ANSWER **FOUR (4)** QUESTIONS ONLY

- Q1** (a) Given a function, $f(t) = 2t^2 \sinh at u(t)$. By using the Laplace Transform definition, determine the Laplace Transform of the time integration $f(t)$. Given that $\sinh x = \frac{1}{2}(e^x - e^{-x})$. (6 marks)
- (b) Obtain the Laplace Transform of the function in Figure **Q1(b)**. (6 marks)
- (c) Determine the time domain function, $i(t)$ for $I(s) = \frac{31s^2 + 8}{s(s+10)(s+9)^2}$. (6marks)
- (d) Find the initial value for the function, $F(s) = \frac{14s^2 + 6}{s(s+1)(s+5)}$. (2 marks)
- Q2** (a) A system has a transfer function, $H(s) = \frac{1}{(s+2)} + \frac{s}{(s^2+4)} - \frac{2}{(s^2+4)}$. Based on the transfer function given,
- (i) plot the poles and zeros diagram. (2 marks)
- (ii) find the output, $y(t)$ if given an input, $x(t) = 2e^{-2t}$. (6 marks)
- (iii) justify if this is a stable system or not. (2 marks)
- (b) The voltage across a 500Ω resistor in a series RLC circuit is $V_R(t) = 10e^{-500t} \sin(3500t)$. How much additional resistance is needed for the response to become critically damped response? (3 marks)
- (c) Convolution is an invaluable tool for the engineer because it provides a means of viewing and characterizing physical systems. Figure **Q2(c)** shows the system's impulse function, $h(t)$ and input, $x(t)$. Find the output, $y(t)$ of the system using convolution integral. (7 marks)

- Q3** (a) Refer to Figure **Q3(a)**, find:
- (i) the resonance frequency, ω_0 . (2 marks)
 - (ii) the transfer function, $\frac{V_o(s)}{V_s(s)}$. (3 marks)
 - (iii) the output voltage, V_o at resonance frequency. (2 marks)
- (b) The transfer function for the circuit in Figure **Q3(b)** is given by $\frac{V_o(s)}{V_s(s)} = \frac{s(s+1)}{(s+10)^2}$,
- (i) draw the magnitude and phase plot for the transfer function, $\frac{V_o(s)}{V_s(s)}$. (8 marks)
 - (ii) find the value of capacitance, C, resistance, R_1 and R_2 . (5 marks)
- Q4** (a) Describe FOUR (4) basic types of filter and sketch its frequency response. (12 marks)
- (b) Given a filter circuit in Figure **Q4(b)**,
- (i) obtain the transfer function. (6 marks)
 - (ii) identify the type of filter the circuit represents, if $R_f = R_i$. (2 marks)

- Q5** (a) Two sets of measurements are made on a two-port resistive circuit. The first set is made with port 2 open-circuited, and the second set is made with port 2 short-circuited. The results are as follows:

| Port 2 open circuited | Port 2 short circuited |
|-----------------------|------------------------|
| $V_1 = 10\text{mV}$ | $V_1 = 24\text{mV}$ |
| $I_1 = 10\mu\text{A}$ | $I_1 = 20\mu\text{A}$ |
| $V_2 = -40\text{V}$ | $I_2 = 1\text{mA}$ |

Find the hybrid (h) parameter for this network.

(12 marks)

- (b) Figure Q5(b) shows the Z parameter equivalent network for non-reciprocal case.

- (i) By using Kirchhoff's Voltage Law, prove the following equations:-

$$V_1 = z_{11}I_1 + z_{12}I_2$$

$$V_2 = z_{21}I_1 + z_{22}I_2$$

(4 marks)

- (ii) Draw and completely label the reciprocal equivalent network.

(2 marks)

- (iii) Define reciprocal properties. Explain the reciprocal condition for impedance and admittance parameter.

(2 marks)

PART B: ANSWER ONE(1) QUESTION ONLY.

- Q6 (a)** Fourier series is used in circuit analysis when the input supplied to a particular network is a type of periodic non-sinusoidal signal. Explain with the aid of a diagram how the principle of superposition is employed in analysing this type of network. (5 marks)

- (b) The circuit parameters of Figure **Q6(b)(i)** are $R = 100 \Omega$, $C = 100 \mu\text{F}$ and $L = 1.2 \text{ mH}$. The input current in Figure **Q6(b)(ii)** is applied to the circuit. It is a half-wave rectified signal having the following Fourier series expansion:

$$i(t) = \frac{1}{100\pi} + \frac{1}{200} \sin \omega t - \frac{1}{150\pi} \cos 2\omega t + \dots \text{ where } \omega = 377 \text{ rad/s.}$$

- (i) Find the first two non-zero terms of the Fourier series expression for the voltage, $v_o(t)$. (11 marks)
- (ii) What would happen to the components of the voltage, $v_o(t)$ if the positions of capacitor and inductor are swapped? Please justify your answer. (4 marks)

- Q7 (a)** Explain how Fourier transform could be determined from Laplace transform. (5 marks)

- (b) An input signals, $v(t) = 10e^{-t}u(t)$ is used to control a valve. The DC component of $v(t)$ is required to actuate the valve while the higher frequency components of $v(t)$ need to be attenuated in order to reduce valve wear. Thus the low pass circuit shown in Figure **Q7(b)** is employed. The circuit is designed so that the magnitude of the output voltage at $\omega = 5 \text{ rad/s}$ is equal to 5 % of the magnitude of the output voltage at $\omega = 0 \text{ rad/s}$.

- (i) Find the Fourier Transform of $v(t)$. (2 marks)
- (ii) Determine the value of inductor, L. (9 marks)
- (iii) Would the circuit behave differently if the output signal, $v_o(t)$ is the voltage across the resistor instead? Justify your answer. (4 marks)

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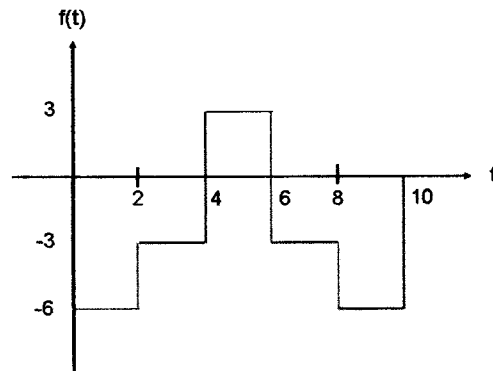


Figure Q1(b)

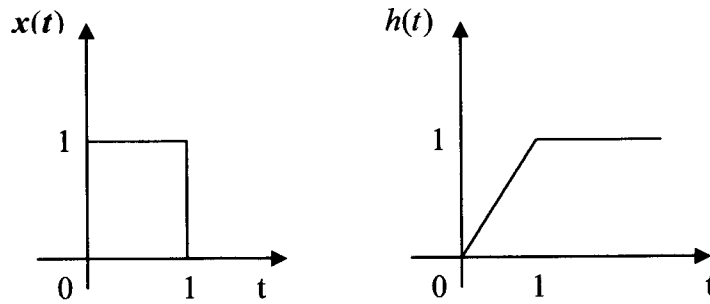


Figure Q2(c)

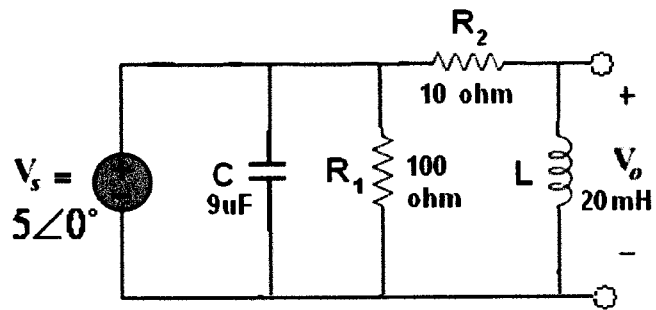


Figure Q3(a)

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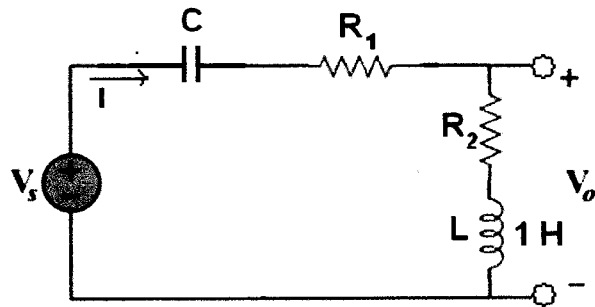


Figure Q3(b)

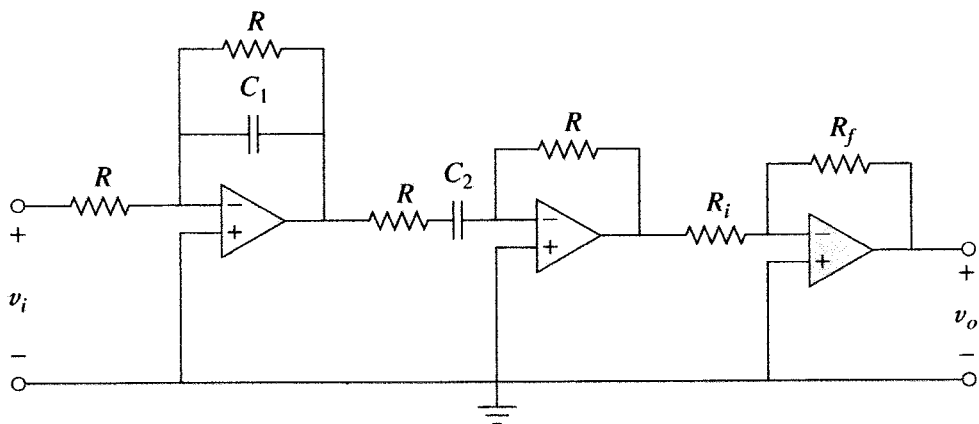


Figure Q4(b)

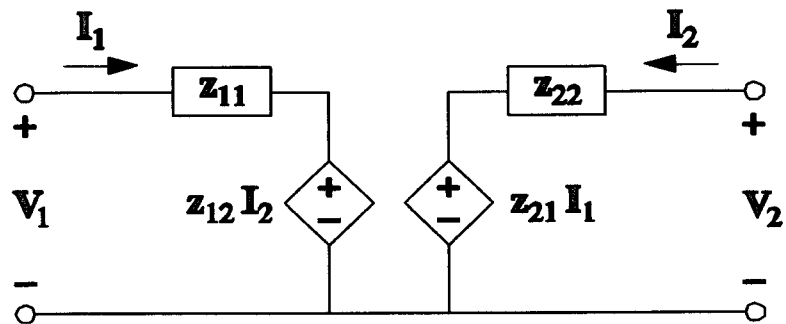


Figure Q5(b)

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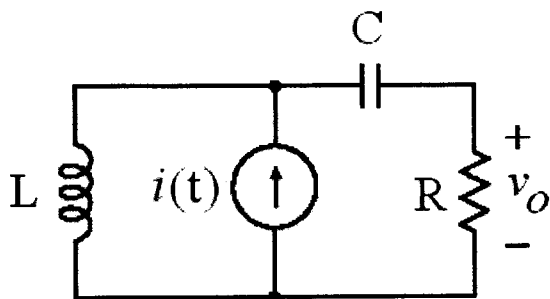


Figure Q6(b)(i)

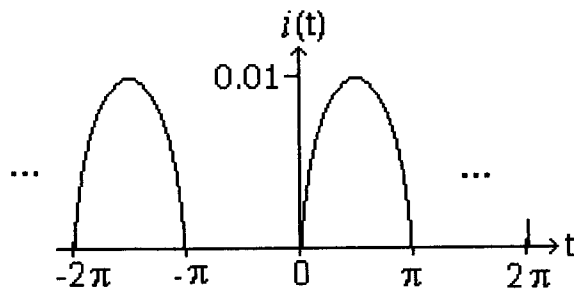


Figure Q6(b)(ii)

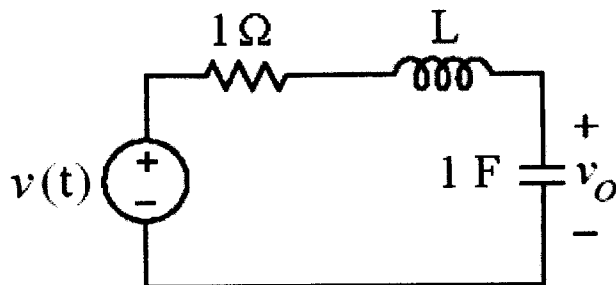


Figure Q7(b)

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| Table 1: Properties of Laplace Transform | | |
|---|---|---|
| No. | f(t) | F(s) |
| 1. | $\delta(t)$ | 1 |
| 2. | $u(t)$ | $1/s$ |
| 3. | $tu(t)$ | $1/s^2$ |
| 4. | $t^n u(t)$ | $(n!)/s^{n+1}$ |
| 5. | $e^{-at} u(t)$ | $1/(s+a)$ |
| 6. | $\sin \omega t u(t)$ | $\omega/(s^2+\omega^2)$ |
| 7. | $\cos \omega t u(t)$ | $s/(s^2+\omega^2)$ |
| 8. | $f(at)$ | $\frac{1}{a} F\left(\frac{s}{a}\right)$ |
| 9. | $e^{-at} f(t)$ | $F(s+a)$ |
| 10. | $f(t-a) u(t-a)$ | $e^{-as} F(s)$ |
| 11. | $\frac{df}{dt}$ $\frac{d^n f}{dt^n}$ | $sF(s) - f(0^-)$ $s^n F(s) - s^{n-1} f(s)$ $- s^{n-2} f'(0^-) \dots - f^{(n-1)}(0^-)$ |
| 12. | $\int_0^t f(t) dt$ | $\frac{1}{s} F(s)$ |
| 13. | $tf(t)$ | $-\frac{d}{ds} F(s)$ |
| 14. | $\frac{f(t)}{t}$ | $\int_0^\infty F(s) ds$ |
| 15. | $f(t+nT)$ | $\frac{F_1(s)}{1 - e^{-sT}}$ |
| 16. | $f(0)$ | $\lim_{s \rightarrow \infty} sF(s)$ |
| 17. | $f(\infty)$ | $\lim_{s \rightarrow 0} sF(s)$ |
| 18. | $f_1(t) * f_2(t)$ | $F_1(s) \cdot F_2(s)$ |