



## **UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

### **FINAL EXAMINATION SEMESTER I SESSION 2009/2010**

SUBJECT NAME : ELECTRIC NETWORK ANALYSIS & SYNTHESIS  
SUBJECT CODE : BEE 3113  
COURSE : 2 & 3 BEE  
EXAMINATION DATE : NOVEMBER 2009  
DURATION : 2  $\frac{1}{2}$  HOURS  
INSTRUCTION : ANSWER FOUR (4) QUESTIONS ONLY.

THIS PAPER CONSISTS OF 12 PAGES

**Q1** Please use Table Q1 for your reference.

(a) Determine the Laplace transform of the following function:

(i)  $f(t) = t^2 \sin(2t)$  (3 marks)

(ii)  $g(t) = te^{-3t}$  (3 marks)

(iii)  $h(t) = \sin at \cos at$  (3 marks)

(b) Obtain the Laplace transforms of the waveform shown in Figure Q1(b).

(6 marks)

(c) Solve the following functions:

(i)  $G(s) = \frac{-2s+1}{(s-1)^2}$  (4 marks)

(ii)  $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + 5y = 0$  Given:  $y = 1$ ,  $\frac{dy}{dt} = 0$  when  $t = 0$ .  
(6 marks)

**Q2** (a) Given a function,  $h(t) = [3 - 3e^{-2t} + 2te^{-2t}]u(t)$ .

(i) Find the transfer function,  $H(s)$  (4 marks)

(ii) Construct a pole-zero map of the waveform  $H(s)$  (3 marks)

(iii) Determine the output,  $y(t)$  if an input of  $x(t) = te^{-3t}u(t)$  is applied to the system. (8 marks)

(b) The convolution integral is used in finding the output response,  $y(t)$  of a system to an excitation input,  $x(t)$ . A linear circuit has an impulse response,  $h(t) = [u(t) - 2u(t-1) - u(t-2)]$  as shown in Figure Q2 (b). An input,  $x(t) = [u(t) - u(t-1)]$  is applied to the linear circuit.

(i) Sketch the input response,  $x(t)$ . (1 mark)

(ii) Find the response,  $y(t)$  using the convolution integral. (9 marks)

- Q3** (a) Explain the impedance characteristic of an RLC series circuit at resonance condition. (4 marks)

- (b) Based on Figure Q3 (b);

(i) Prove the resonant frequency,  $\omega_n$  is given by  $\omega_n = \frac{1}{\sqrt{LC}} \sqrt{1 - \frac{L}{R_2^2 C}}$ .

(6 marks)

- (ii) Determine the resonant frequency  $\omega_n$  if the value of  $R_1=1k\Omega$ ,  $R_2=10k\Omega$ ,  $L=1mH$  and  $C=0.4uF$ . (3 marks)

- (c) Based on Figure Q3 (c);

(i) Find the transfer function  $H(s) = \frac{I_0}{V_s}$ .

(4 marks)

- (ii) Construct the Bode magnitude and phase plots for H(s). (8 marks)

- Q4**
- (a) State the definition of frequency selective filter. (1 mark)
  - (b) Name two different groups of filters. For each group, list two (2) advantages and two (2) disadvantages offered by them. (10 marks)
  - (c) Using a table, explain 4 basic types of filter and sketch its frequency response. (8 marks)
  - (d) Determine the values of inductor and resistor to design an RLC band stop filter given the  $f_0 = 8 \text{ kHz}$ ,  $C = 500 \text{ nF}$  and  $Q = 6$ . (6 marks)

- Q5** (a) Find the  $h$  parameters for the two port network shown in Figure Q5(a). Use the following values:  $R_1=2\Omega$ ,  $L_1=2H$ ,  $L_2= 1H$  and  $C_1=2F$ .  
(10 marks)

- (b) A linear network has  $y$  parameters as below.

$$y = \begin{bmatrix} 0.75 & -0.5 \\ -0.5 & 0.625 \end{bmatrix} S$$

- (i) Find the resistive circuit.  
(7 marks)

- (ii) Determine the  $z$  parameters and draw the equivalent circuit.  
(8 marks)

**Q6** (a) (i) State the definition of Exponential Fourier Series. (2 marks)

- (ii) Determine the Exponential Fourier Series of the waveform shown in Figure Q6(a)(ii). Plot the magnitude spectrum of this waveform (from  $n = -4$  to  $n = 4$ ) and label the diagram. What can be deduced from the observation of magnitude spectrum? (9 marks)

- (b) The input current to the circuit shown in Figure Q6(b) is a sawtooth wave having the following Fourier series expansion:

$$i(t) = \frac{1}{2} - \frac{1}{\pi} \sin(\pi t) - \frac{1}{2\pi} \sin(2\pi t) - \frac{1}{3\pi} \sin(3\pi t) - \dots$$

The circuit is designed to produce the output voltage,  $v_o(t)$  so that the magnitude of the fundamental component is 80 % less than the magnitude of the input signal.

- (i) Determine the value of inductor. (6 marks)

- (ii) Find the first three (3) nonzero terms of the output signal,  $v_o(t)$  using the value of inductor obtained in part (b)(i). (8 marks)

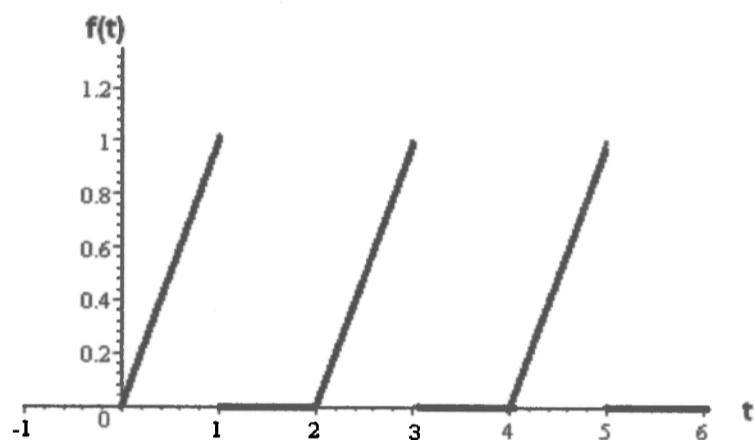
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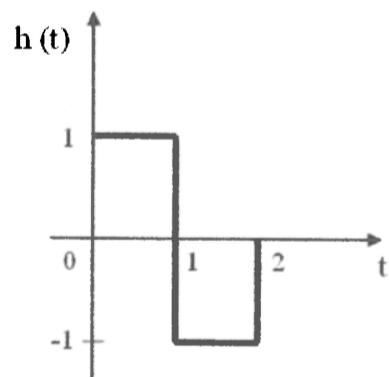
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**Figure O1 (b)**



**Figure O2 (b)**

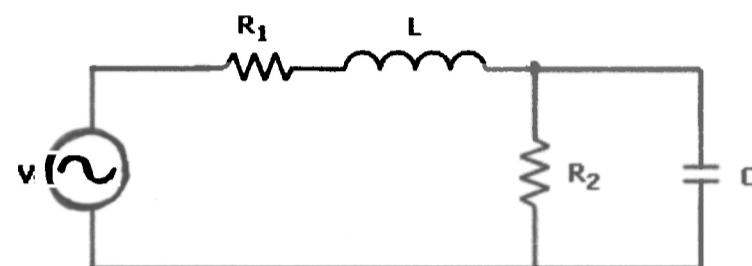
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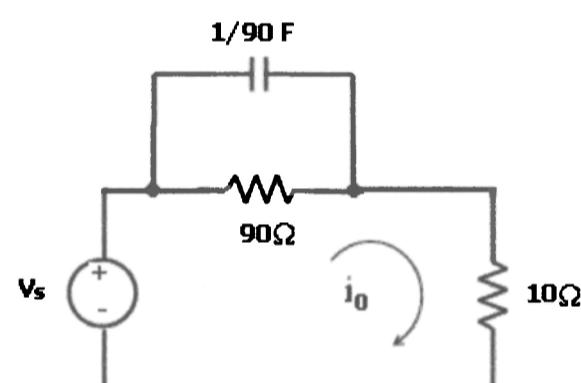
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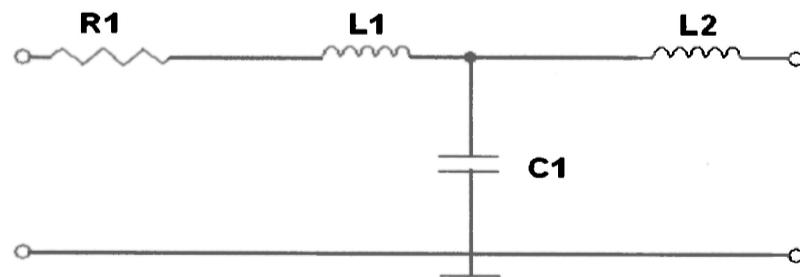
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**Figure Q3 (b)**



**Figure Q3 (c)**



**Figure Q5 (a)**

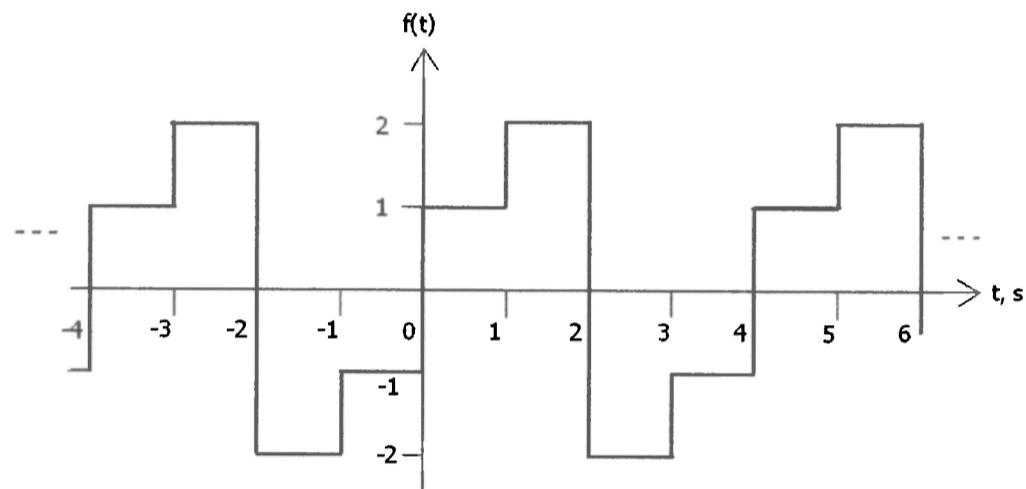
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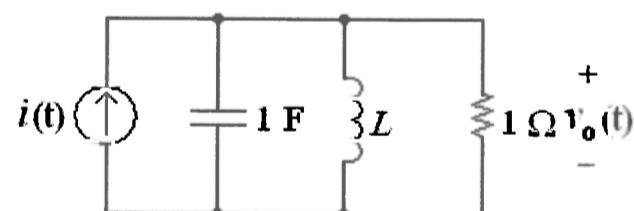
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**Figure O6(a)(ii)**



**Figure O6(b)**

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Table 1: Properties of Laplace Transform

No.	$f(t)$	$F(s)$
1.	$\delta(t)$	1
2.	$u(t)$	$1/s$
3.	$tu(t)$	$1/s^2$
4.	$t^n u(t)$	$(n!)/s^{n+1}$
5.	$e^{-at} u(t)$	$1/(s+a)$
6.	$\sin \omega t u(t)$	$\omega/(s^2+\omega^2)$
7.	$\cos \omega t u(t)$	$s/(s^2+\omega^2)$
8.	$f(at)$	$\frac{1}{a} F(\frac{s}{a})$
9.	$e^{-at} f(t)$	$F(s+a)$
10.	$f(t-a) u(t-a)$	$e^{-as} F(s)$
11.	$\frac{df}{dt}$	$sF(s) - f(0^-)$
	$\frac{d^n f}{dt^n}$	$s^n F(s) - s^{n-1} f(s) - s^{n-2} f'(0) - \dots - f^{(n-1)}(0^-)$
12.	$\int_0^t f(t) dt$	$\frac{1}{s} F(s)$
13.	$tf(t)$	$-\frac{d}{ds} F(s)$
14.	$\frac{f(t)}{t}$	$\int_s^\infty F(s) ds$
15.	$f(t+nT)$	$\frac{F(s)}{1-e^{-sT}}$
16.	$f(0)$	$\lim_{s \rightarrow \infty} sF(s)$
17.	$f(\infty)$	$\lim_{s \rightarrow 0} sF(s)$
18.	$f_1(t)*f_2(t)$	$F_1(s).F_2(s)$

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Table 2: Trigonometric Integrals

$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
$\sin A \cos A = \frac{1}{2} \sin 2A$
$\int_0^T \sin n\omega_o t \ dt = 0$
$\int_0^T \cos n\omega_o t \ dt = 0$
$\int_0^T \sin n\omega_o t \ \cos m\omega_o t \ dt = 0$
$\int_0^T \sin n\omega_o t \ \sin m\omega_o t \ dt = 0, \quad (m \neq n)$
$\int_0^T \cos n\omega_o t \ \cos m\omega_o t \ dt = 0, \quad (m \neq n)$
$\int_0^T \sin^2 n\omega_o t \ dt = T/2$
$\int_0^T \cos^2 n\omega_o t \ dt = T/2$

Table 3: Fourier Transform Pairs

Pair	$f(t)$	$F(\omega)$
1	$\delta(t)$	1
2	$A$	$2\pi A \delta(\omega)$
3	$\text{sgn}(t)$	$2/j\omega$
4	$u(t)$	$\pi\delta(\omega) + 1/j\omega$
5	$e^{-at} u(t)$	$1/(a + j\omega), a > 0$
6	$e^{at} u(-t)$	$1/(a - j\omega), a > 0$
7	$e^{-a t }$	$2a/(a^2 + \omega^2), a > 0$
8	$e^{j\omega_0 t}$	$2\pi\delta(\omega - \omega_0)$
9	$\cos(\omega_0 t)$	$\pi[\delta(\omega + \omega_0) + \delta(\omega - \omega_0)]$
10	$\sin(\omega_0 t)$	$j\pi[\delta(\omega + \omega_0) - \delta(\omega - \omega_0)]$