

**CONFIDENTIAL**



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER 2  
SESSION 2010/2011**

NAME OF COURSE : DYNAMICS  
COURSE CODE : BDA 20103 / BDA 2013  
PROGRAM : BACHELOR OF MECHANICAL  
ENGINEERING WITH HONOURS  
DATE OF EXAMINATION : APRIL / MAY 2011  
DURATION : 3 HOURS  
INSTRUCTION : ANSWER ALL QUESTIONS.

THIS PAPER CONSISTS OF NINE (9) PAGES

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- Q1 (a)** **Figure Q1(a)** shows a diagram of a rigid body which is undergoing rotation about a fixed axis. Derive the equations which represent the magnitude of velocity and acceleration of point P by using the  $x$ - $y$  coordinate system.

[5 marks]

- (b)** A large window AB is closed by using the power window system through the application of cable as shown in **Figure Q1(b)**. The window has the width of 3 m and the roller which connect the window and the wall is positioned at 1.5m from point A. If the cable is pulled by the force F with a constant speed of 0.8 m/s at the instant theta is equal to 55 degrees ( $\theta = 55^\circ$ );

- (i) Determine the position coordinate equation which represents the motion of the system.
- (ii) Find the distance  $x$  at the instant  $\theta = 55^\circ$ .
- (iii) Calculate the angular velocity of the large window AB.
- (iv) Find the angular acceleration of the large window AB.

[15 marks]

- Q2 (a)** The link shown in **Figure Q2 (a)** is guided by two block A and B, which move in the fixed slots. The velocity of block A is 4 m/s downward.

- (i) Draw kinematics diagram of the body.
- (ii) Determine the magnitudes  $v_B$  and  $\omega$  using the velocity equation of  $v_B = v_A + v_{B/A}$  to points A and B.

[6 marks]

- (b) The connecting rod ABD is fixed at A and the length of rod AB and BD is 0.8 m respectively. Block D shown in **Figure Q2 (b)** moves with a speed of 6 m/s.
- (i) Show the location of the instantaneous center (IC) on the kinematics diagram of link BD.
  - (ii) Determine the angular velocity of link BD.
  - (iii) Determine the velocity of B.
  - (iv) Draw the kinematics diagram of link AB.
  - (v) Determine the angular velocity of AB.

[14 marks]

**Q3** **Figure Q3** shows that pin A is fixed on bar DC. At the position shown, the bar DC is rotating counterclockwise at the constant rate,  $\omega_{DC} = 2 \text{ rad/s}$ . Pin A can only slide along the slotted plate EBO. Assume P be a point on EBO coincident with A. At this instant,

- (a) Determine the angular velocity of EBO,  $\omega_{EBO} \text{ rad/s}$ .

[7marks]

- (b) Determine the angular acceleration of EBO,  $\alpha_{EBO} \text{ rad/s}^2$ .

[8 marks]

- (c) Draw the velocity and acceleration diagrams

[5 marks]

**Q4** A plate structure as seen in **Figure Q4** has a pin rotation at O and simply supported at A. This plate structure is made of material with the density of  $7800\text{kg/m}^3$ . The thickness of the plate is 5mm.

- (a) Find the location of the center of mass (center of gravity) of the plate structure, measured from the pin rotation O. [8 marks]
- (b) Calculate the reaction force at the support A. [5 marks]
- (c) If the plate structure has only pin support O without another support at A, Find the moment at O to hold the plate structure at still. [7 marks]

**Q5** A 3.5 kg slender bar AB rotates (clockwise direction) about the pivot rotation at O starting at vertical position with initial angular velocity of 2 rad/s as shown in **Figure Q5**. A soft spring with a constant of 200 N/m is attached at the initial position. The original length of the spring is 120mm.

- (a) Determine the inertia of the slender bar about the point of rotation (point O). [5 marks]
- (b) Calculate the change of kinetic energy after the slender bar has rotated  $90^\circ$ . [5 marks]
- (c) Calculate the change of total potential energy after the slender bar has rotated  $90^\circ$ . [5 marks]
- (d) Find the angular velocity of the slender bar about the pivot of rotation O. [5 marks]

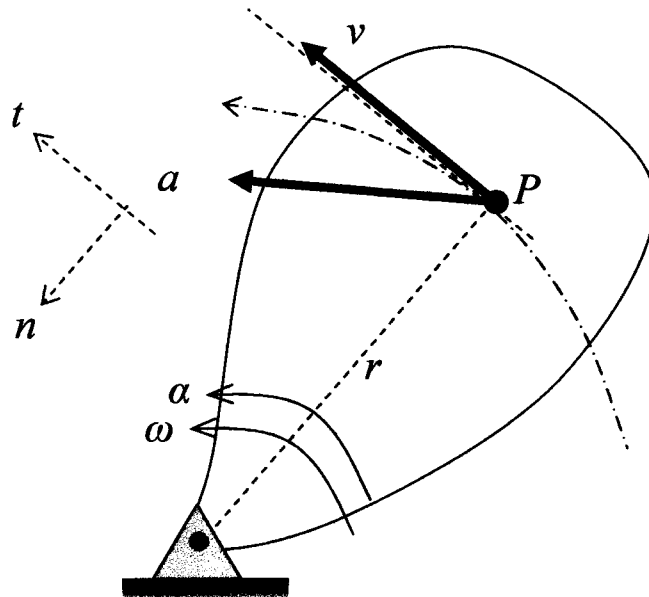
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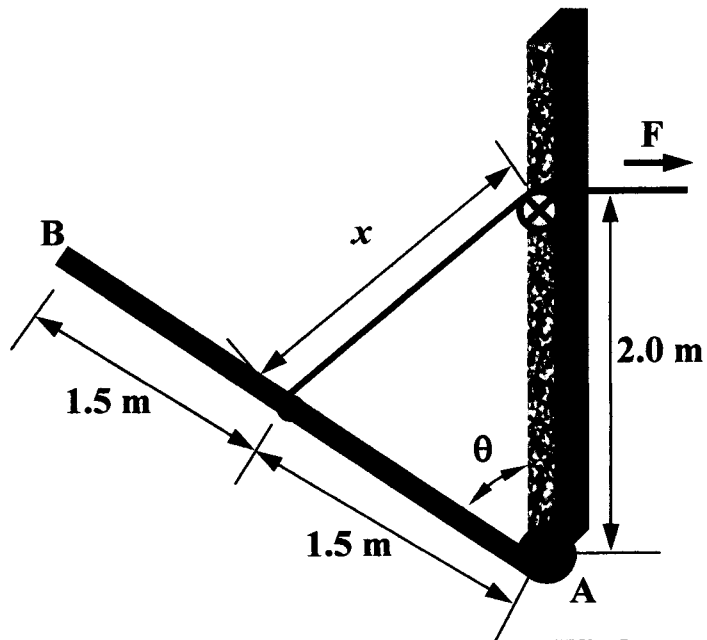
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**Figure Q1(a): Fixed Axis Rotation**



**Figure Q1(b): Motion of Large Window**

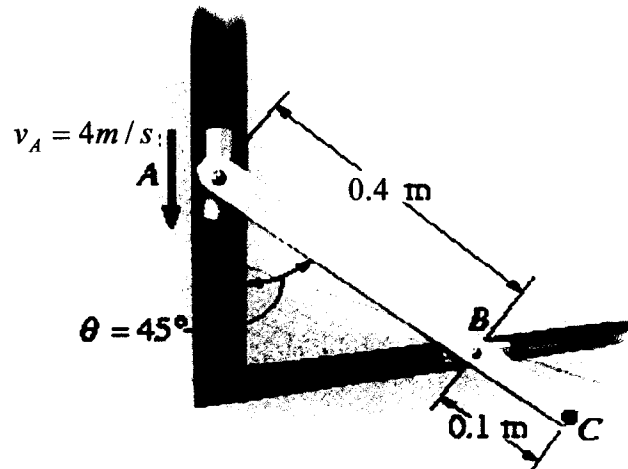
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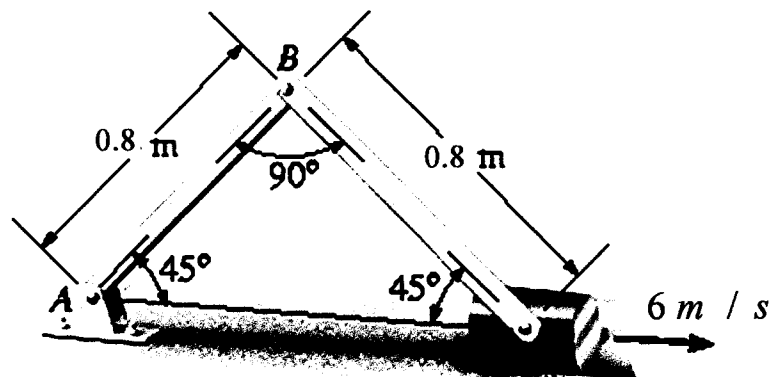
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**Figure Q2(a): Link on the Fixed Slot**



**Figure Q2(b): Connecting Rod and Block D**

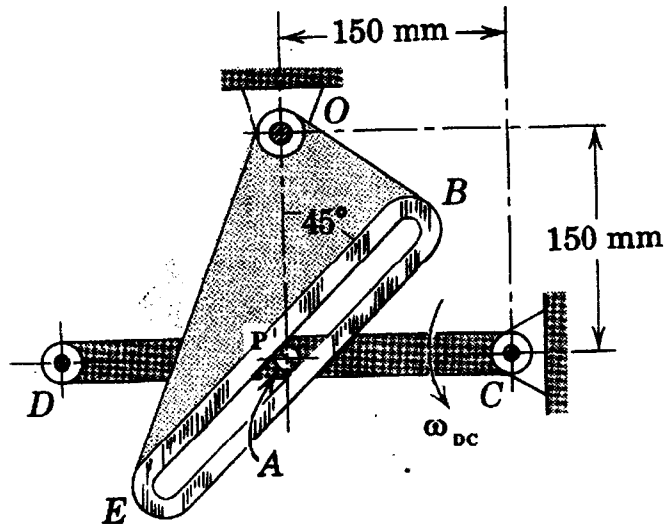
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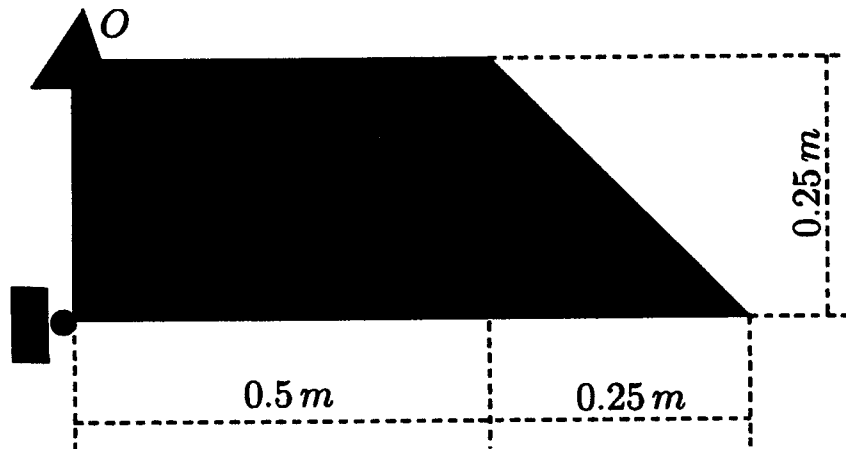
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**Figure Q3: Bar and Slotted Plate**



**Figure Q4: Plate Structure**

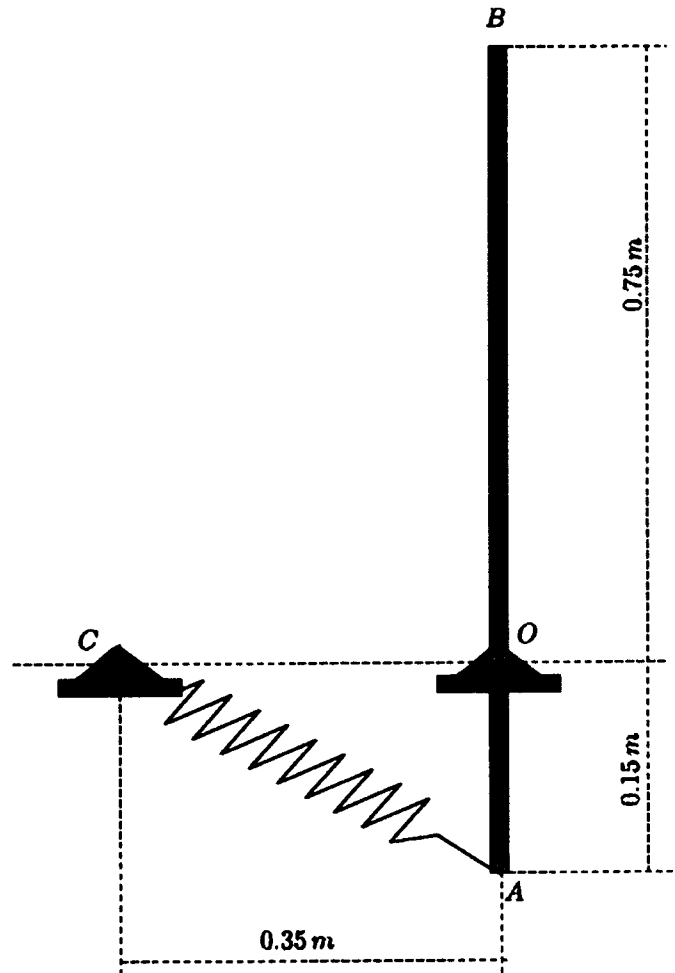
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**Figure Q5: Rotating Slender Bar**



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$$s = s_0 + v_0 t + \frac{1}{2} a t^2$$

$$v = v_0 + a t$$

$$v^2 = v_0^2 + 2 a s$$

$$\theta = \theta_0 + \omega t + \frac{1}{2} \alpha t^2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + 2 \alpha s$$

$$\mathbf{v} = \mathbf{v}^r + \mathbf{v}^\theta$$

$$\mathbf{v}^\theta = r \omega \quad \mathbf{v}^r = \dot{r}$$

$$\mathbf{a} = \mathbf{a}^r + \mathbf{a}^\theta$$

$$\mathbf{a}^r = \ddot{r} - \dot{\theta}^2 r$$

$$\mathbf{a}^\theta = \ddot{\theta} r + 2 \dot{\theta} \dot{r}$$

$$\mathbf{a} = \mathbf{a}^n + \mathbf{a}^t$$

$$\mathbf{a}^n = r \omega^2 = \frac{v^2}{r}$$

$$\mathbf{a}^t = r \alpha$$

$$T_1 + U_{1 \rightarrow 2} = T_2$$

$$T_1 + V_1 = T_2 + V_2$$

$$U = \Delta T + \Delta V_g + \Delta V_e$$

$$\Delta T = \frac{1}{2} m (v_2^2 - v_1^2) + \frac{1}{2} I_G (\omega_2^2 - \omega_1^2)$$

$$\Delta V_g = m g (h_2 - h_1)$$

$$\Delta V_e = \frac{1}{2} k (x_2^2 - x_1^2)$$

$$m v_1 + \sum_{t_1}^{t_2} \int F dt = m v_2$$

$$(H_0)_1 + \sum_{t_1}^{t_2} \int M_0 dt = (H_0)_2$$

$$m_A (v_A)_1 + m_B (v_B)_1 = m_A (v_A)_2 + m_B (v_B)_2$$

$$I_G \omega_1 + m (v_G)_1 d_1 + \sum \int M_A dt = I_G \omega_2 + m (v_G)_2 d_2$$

$$e = - \frac{(v_B)_2^n - (v_A)_2^n}{(v_B)_1^n - (v_A)_1^n}$$

$$(v_A)_1^t = (v_A)_2^t$$

$$\sum M_G = I_G \alpha$$

$$\sum F = m a$$

$$\mathbf{v}_P = \mathbf{v}_{P'} + \mathbf{v}_{P/Oxy}$$

$$\mathbf{v}_P = (\dot{\mathbf{r}})_{OXY} = \boldsymbol{\Omega} \times \mathbf{r} + (\dot{\mathbf{r}})_{Oxy}$$

$$\mathbf{a}_P = \mathbf{a}_{P'} + \mathbf{a}_{P/Oxy} + \mathbf{a}_C$$

$$\mathbf{a}_P = \boldsymbol{\Omega} \times (\boldsymbol{\Omega} \times \mathbf{r}) + \dot{\boldsymbol{\Omega}} \times \mathbf{r} + 2(\boldsymbol{\Omega} \times (\dot{\mathbf{r}})_{Oxy}) + (\ddot{\mathbf{r}})_{Oxy}$$

$$I = m k_G^2$$

$$I = \int_m r^2 dm$$

$$I_x = \frac{1}{18} m h^2$$

$$I_y = \frac{1}{18} m b^2$$

$$I_z = \frac{1}{18} m (b^2 + h^2)$$

$$I_{xx} = I_{yy} = \frac{1}{12} m l^2$$

$$I_{x'x'} = \frac{1}{3} m l^2$$

$$I_{xx} = \frac{1}{12} m (B^2 + C^2)$$

$$I_{yy} = \frac{1}{12} m (A^2 + B^2)$$

$$I_{zz} = \frac{1}{12} m (A^2 + C^2)$$

