

# UNIVERSITI TUN HUSSEIN ONN MALAYSIA

# FINAL EXAMINATION SEMESTER I SESSION 2014/2015

**COURSE NAME** 

PRESTRESSED CONCRETE

**DESIGN** 

**COURSE CODE** 

BFS 40303

**PROGRAMME** 

4 BFF

EXAMINATION DATE

DECEMBER 2014/JANUARY 2015

**DURATION** 

3 HOURS

INSTRUCTION

ANSWER FOUR (4) QUESTIONS

**ONLY** 

THIS QUESTION PAPER CONSISTS OF NINE (9) PAGES

Q1 (a) Discuss THREE (3) main advantages of using prestressed concrete.

(6 marks)

(b) A simply supported pre-tensioned concrete beam with span 12 m and has a rectangular cross section of 450 mm wide and 650 mm overall depth. The beam is prestressed with 10 numbers of 15.2 mm diameter straight strands, each with a nominal cross sectional area of 139 mm<sup>2</sup>. The beam carries no dead load other than its own weight and all surfaces are exposed to the environment having an average relative humidity of 75%. The following information is given:

Young's Modulus of tendon,  $E_{ps}$  = 195 GPa Young's Modulus of Concrete,  $E_c$  = 35 GPa Initial prestressing stress,  $\sigma_{pi}$  = 1150 MPa Strength of tendon,  $f_{pu}$  = 1670 MPa

Calculate the long term loss of prestress due to shrinkage and creep.

(19 marks)

Q2 A post-tensioned prestressed concrete bridge deck is in the form of a solid slab as shown in Figure Q2. The bridge deck is simply supported over 20 m. It carries a service load of 0.3 kN/m<sup>2</sup>. The allowable concrete stresses are given below:

Allowable compressive stress at transfer,  $f'_{max}$  = 20 MPa Allowable compressive stress at service,  $f_{max}$  = 16.7 MPa Allowable tensile stress at transfer,  $f'_{min}$  = -1.0 MPa Allowable tensile stress at service,  $f_{min}$  = 0 MPa

(a) If the total short-term and long –term losses are 10% and 20%, respectively, determine the minimum depth of slab required.

(13 marks)

(b) If the depth of the deck slab is 525 mm and the maximum eccentricity of the tendons at mid-span is 75 mm above the soffit, find the minimum value of the prestress force required.

(12 marks)

- A bonded prestressed concrete beam is of T section is shown in Figure Q3. The tendon consists of 3300 mm<sup>2</sup> of standard strands with the characteristic strength of 1700 N/mm<sup>2</sup> and Young's Modulus equal to 200 kN/mm<sup>2</sup> was stressed to an effective prestress of 910 N/mm<sup>2</sup>. The strands are located 870 mm from the top face of the beam. The concrete characteristic strength is 60 N/mm<sup>2</sup> and its modulus of elasticity is 36 kN/mm<sup>2</sup>. Assume the neutral axis is in the web.
  - (a) Calculate the ultimate moment of resistance of the beam section based on the first principles.

(17 marks)

(b) Due to the site error, the strands have not been tensioned (the effective tendon prestress is zero). Calculate the ultimate moment of resistance of the beam section.

(8 marks)

Q4 A prestressed concrete girder, simply supported over a span of 20 m has been designed for flexure to carry in addition to its own weight, a characteristic dead load and live load of 4.5 kN/m and 10 kN/m, respectively. The beam is pre-tensioned with 16 numbers of 15.7 mm diameter strands with nominal cross sectional area of each strand,  $A_{ps} = 150 \text{ mm}^2$ . However, due to debonding only 8 of the strands are active at a section 3 m from the support (Figure Q4). These 8 strands supply an effective prestressing force of 1200 kN. Given the following additional information:

Cross sectional area of concrete,  $A_c$  = 324,000 mm<sup>2</sup> Second moment of area, I = 38.1 x 10<sup>9</sup> mm<sup>4</sup>  $y_b$  of the cross section = 445 mm Strength of concrete,  $f_{cu}$  = 40 MPa Strength of steel,  $f_{yv}$  = 250 MPa Ratio of  $\sigma_{pe}/f_{pu}$  = 0.56

If the section is cracked in flexure, design the shear reinforcement at a distance 3 m from the support. Use 10 mm diameter shear reinforcement.

(25 marks)

Q5 (a) Figure Q5(a) shows a end block containing a single, centrally placed anchorage with a bearing plate of height, h. The beam analogy model together with the shear force and bending moment diagrams for the end block is shown in Figure Q5(a)(ii). Prove that the bursting tension force, T<sub>b</sub> as,

$$T_b = (F/4)(1-h/D)$$
 (12 marks)

(b) Two horizontal tendons are symmetrically anchored in a rectangular end block 400 mm wide and 1000 mm deep. The anchorages have 220 mm square bearing plates and are placed 600 mm apart is divided into two prisms as shown in Figure Q5(b). The maximum jacking force at transfer of prestress is 1400 kN in each tendon. The allowable stress of steel is 200 N/mm<sup>2</sup>. Design the reinforcement for the end block.

(13 marks)

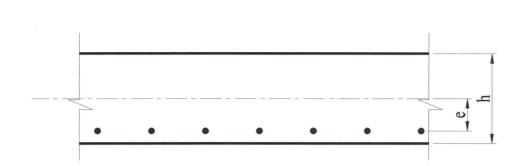
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# FIGURE Q2

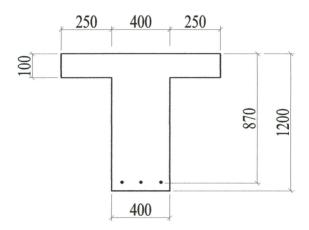


FIGURE Q3

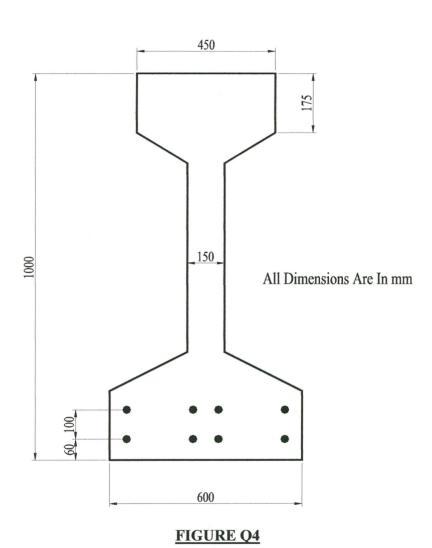
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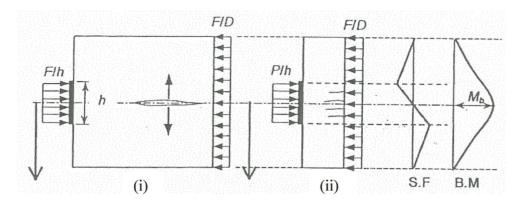
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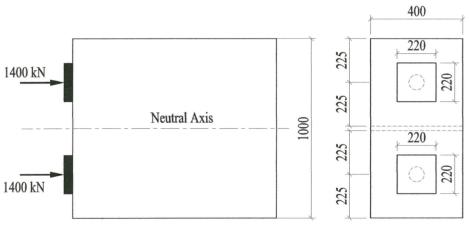
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# FIGRURE Q5(a)



All units are in mm

# FIGRURE Q5(b)

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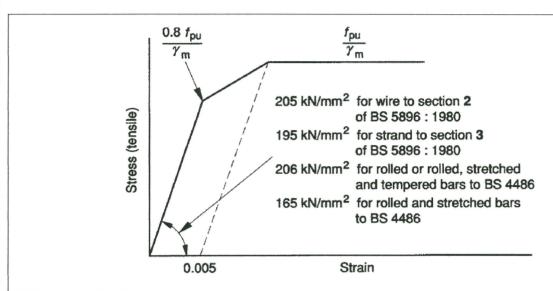
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#### **APPENDIX**

# (A) Stress-Strain Curve of Prestressing Tendons



NOTE  $f_{pu}$  is in N/mm<sup>2</sup>.

### (B) Bursting Forces in End-Blocks

y <sub>po</sub> /y <sub>o</sub>	0.2	0.3	0.4	0.5	0.6	0.7
F <sub>bst</sub> /P <sub>i</sub>	0.23	0.23	0.20	0.17	0.14	0.11

y<sub>o</sub> is half the side of the end block

 $y_{po}$  is half the side of the loaded area

P<sub>i</sub> is the tendon jacking force

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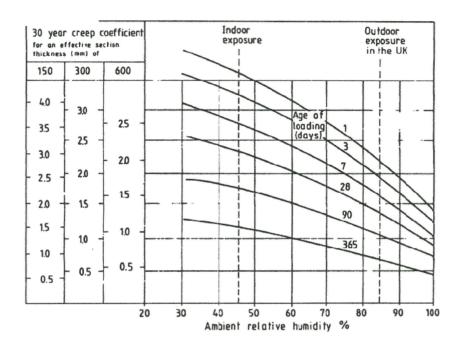
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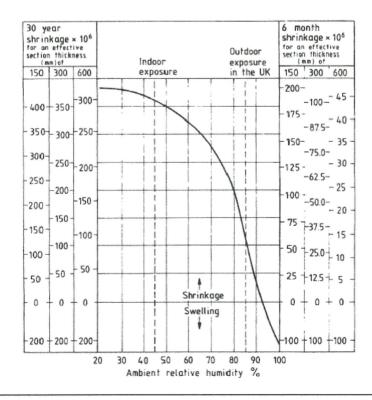
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### (C) Creep Coefficient, φ



## (D) Drying Shrinkage of Normal-Weight Concrete



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### (E) Strain Compatibility Analysis

$$\varepsilon_{pb} = \varepsilon_{pe} + \varepsilon_{pa}$$

$$\varepsilon_{pe} = \frac{\beta P}{A_{ps} E_s}$$

$$\varepsilon_{pa} = \beta_1 \varepsilon_e + \beta_2 \varepsilon_u$$

Where;

 $\beta_1$  and  $\beta_2$  = bond coefficients

 $\beta_1$  and  $\beta_2 = 1.0$  for fully bonded tendon

 $\varepsilon_e = \frac{1}{E_o}$  x stress in concrete at tendon level due to effective prestress.

$$\varepsilon_{e} = \frac{\beta}{E_{c}} \left[ \frac{P}{A} + \frac{Pe^{2}}{I} \right]$$

$$x = \left[ \frac{\beta_{2}\varepsilon_{cu}}{\beta_{2}\varepsilon_{cu} + \varepsilon_{pb} - \varepsilon_{pe} - \beta_{1}\varepsilon_{e}} \right] d$$

For rectangular section and flange section with neutral axis in the flange;

$$f_{pb} = \frac{0.4 f_{cu}bd}{A_{ps}} \left[ \frac{\beta_2 \varepsilon_{cu}}{\beta_2 \varepsilon_{cu} + \varepsilon_{pb} - \varepsilon_{pe} - \beta_1 \varepsilon_e} \right]$$
$$M_u = A_{ps} f_{pb} (d - 0.45x)$$

For flange section with neutral axis in the web:-

$$M_u = 0.4 f_{cu} b_w x (d-0.45x) + 0.45 f_{cu} (b-b_w) h_f (d-0.5h_f)$$