



UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
SEMESTER II
SESSION 2011/2012**

COURSE NAME : ADVANCED STRUCTURAL ANALYSIS

COURSE CODE : BFS 4013 / BFS 40103

PROGRAMME : BFF

EXAMINATION DATE : JUNE 2012

DURATION : 3 HOURS

INSTRUCTION : ANSWER **FOUR (4)** QUESTIONS ONLY

THIS QUESTION PAPER CONSISTS OF **NINE (9)** PAGES

- Q1** (a) What are the causes of instability of a structure? (5 marks)
- (b) Give **Two (2)** advantages of using the indeterminate structure in the construction industry. (5 marks)
- (c) For the system shown in Figure **Q1**, generate the [b] matrix such that $\{P\} = [b]\{F\}$. (15 marks)

- Q2** For the two member truss shown in Figure **Q2**;
- (a) Determine the global stiffness matrix, K. (8 marks)
- (b) Determine the displacements at joint 2. (9 marks)
- (c) Determine the reactions at each support. (8 marks)

- Q3** (a) Using the basic equation for the curvature of an elastic beam expressed below, derive the formula for critical load of axially loaded simply supported beam as shown in Figure **Q3**.

$$\frac{d^2 y}{dx^2} = \frac{M}{EI}$$

(13 marks)

- (b) Derive the Euler equation for:
- i. Column with one end fixed and one end pinned
 - ii. Column with both end fixed.

Use sketches to support your answer.

(12 marks)

- Q4** (a) Sketch the yield line pattern for the slabs shown in Figure **Q4(a)**. (6 marks)
- (b) The reinforced concrete slab shown in Figure **Q4(b)** is designed to have an ultimate load capacity of 11.3 kN/m^2 across its complete area. Based on the yield line pattern given, determine the ultimate resistance moment. (19 marks)
- Q5** (a) What are the differences between the shape factor and load factor? (5marks)
- (b) Figure **Q5** shows a simply supported beam which carries the load at points B and C. Determine the collapse load of the beam by using virtual work method. (20 marks)

- S1** (a) Apakah sebab berlakunya ketidakseimbangan struktur? (5 markah)
- (b) Berikan **Dua (2)** kelebihan menggunakan struktur tidaktentu statik dalam industri pembinaan. (5 markah)
- (c) Bagi sistem rangka dalam Rajah **Q1**, dapatkan matriks $[b]$ supaya $\{P\}=[b]\{F\}$ (15 markah)

S2 Bagi kekuda dengan dua anggota kekuda seperti dalam Rajah **Q2**;

- (a) Dapatkan matriks kekakuan global, K . (8 markah)
- (b) Dapatkan anjakan pada joint 2. (9 markah)
- (c) Dapatkan daya-daya tindakbalas pada setiap penyokong. (8 markah)

- S3** (a) Dengan menggunakan formula asas lenturan elastik bagi rasuk dibawah, terbitkan formula bagi bean kritikal untuk rasuk mudah yang dibebankan dengan beban paksi seperti dalam Rajah **Q3**.

$$\frac{d^2 y}{dx^2} = \frac{M}{EI}$$

(13 markah)

- (b) Terbitkan persamaan Euler bagi:
- i. Tiang dengan satu hujung pin dan satu hujung terikat tegar
 - ii. Tiang dengan kedua-dua hujung terikat tegar

Gunakan lakaran bagi menyokong jawapan anda.

(12 markah)

- S4** (a) Lakarkan bentuk garisan alah bagi setiap papak dalam Rajah **Q4(a)** (6 markah)
- (b) Rajah **Q4(b)** menunjukkan papak konkrit bertetulang yang direkabentuk untuk menampung kapasiti beban muktamad 11.3 kN/m^2 . Berdasarkan bentuk garisan alah yang diberikan, tentukan momen rintangan muktamad. (19 markah)
- S5** (a) Apakah perbezaan antara faktor bentuk dan faktor beban? (5 markah)
- (b) Rajah **Q5** menunjukkan satu rasuk disokong mudah yang dikenakan beban tumpu pada titik B dan C. Dengan menggunakan kaedah kerja maya, tentukan beban musnah bagi rasuk tersebut. (20 markah)

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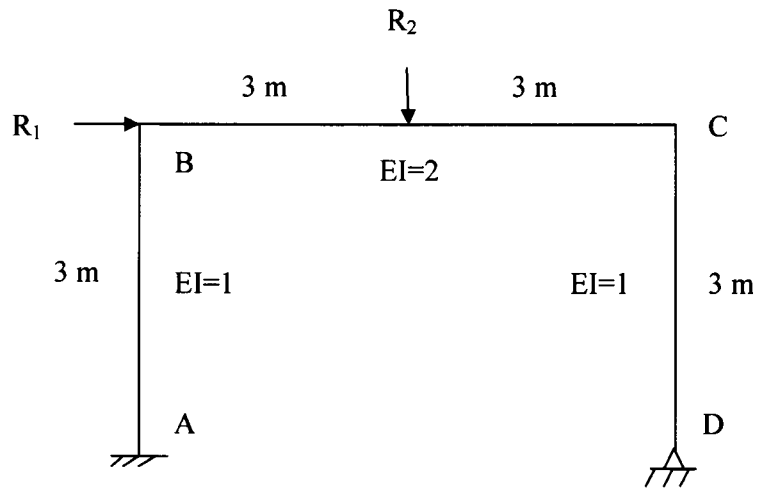


FIGURE Q1

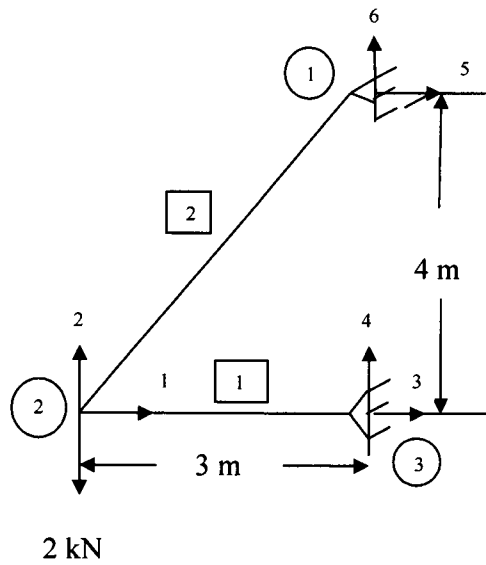


FIGURE Q2

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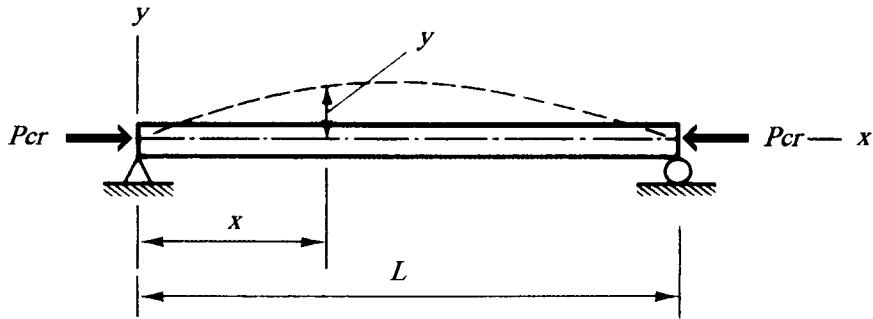


FIGURE Q3

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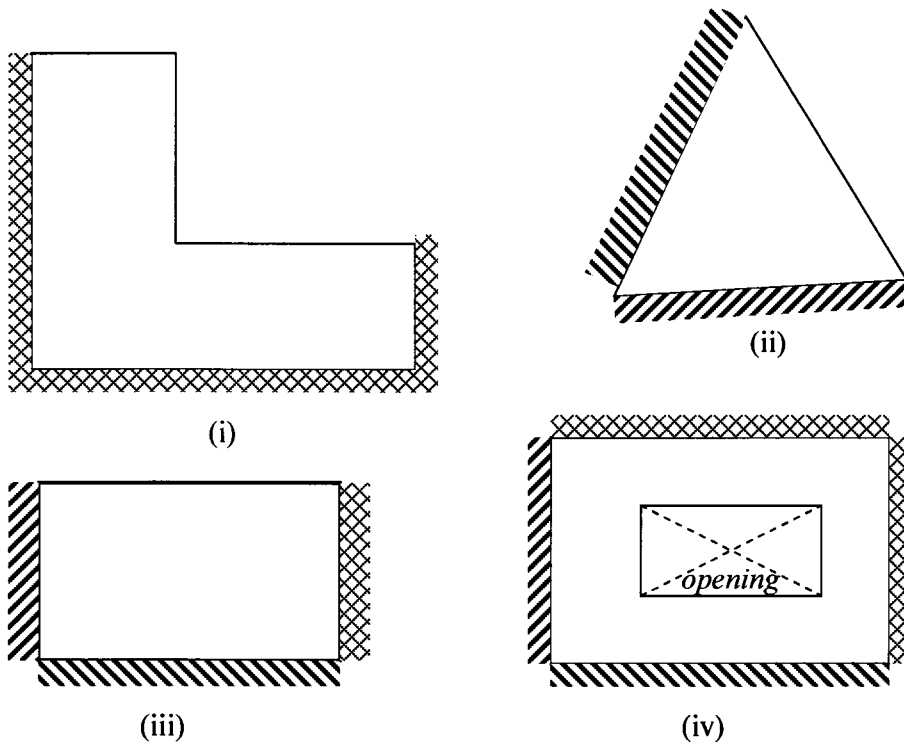


FIGURE Q4(a)

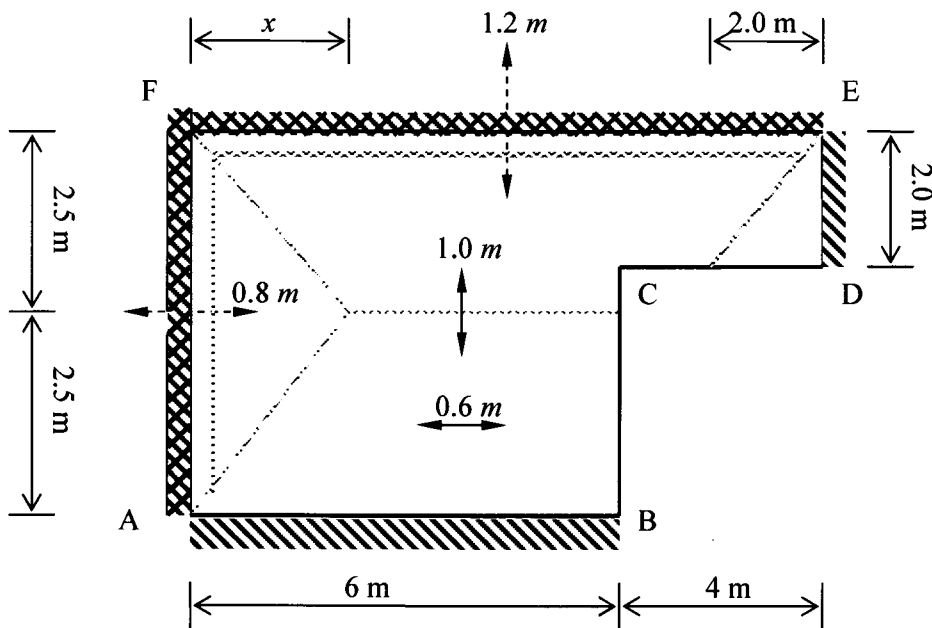


FIGURE Q4(b)

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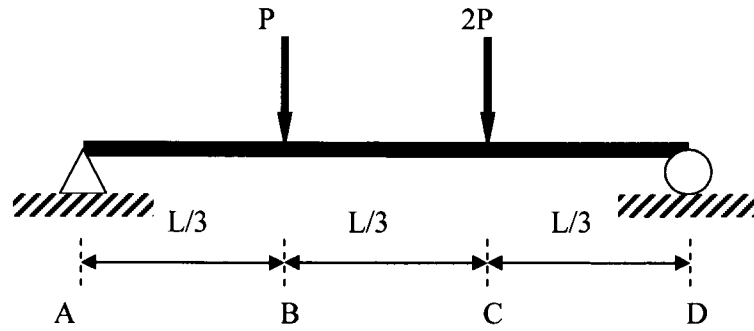
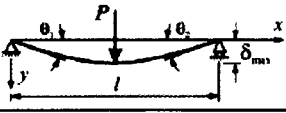
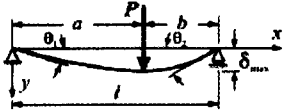
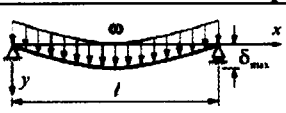
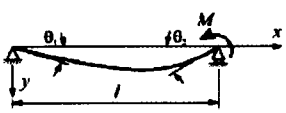
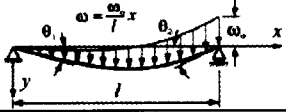
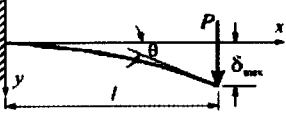
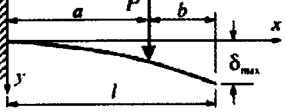
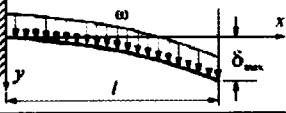
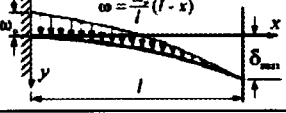
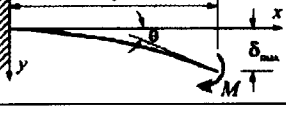


FIGURE Q5

BFS 40103: ADVANCED STRUCTURE ANALYSIS

1) BEAM DEFLECTION FORMULAS

BEAM TYPE	SLOPE AT ENDS	DEFLECTION AT ANY SECTION IN TERMS OF x	MAXIMUM AND CENTER DEFLECTION
6. Beam Simply Supported at Ends – Concentrated load P at the center			
	$\theta_1 = \theta_2 = \frac{Pl^2}{16EI}$	$y = \frac{Px}{12EI} \left(\frac{3l^2}{4} - x^2 \right)$ for $0 < x < \frac{l}{2}$	$\delta_{max} = \frac{Pl^3}{48EI}$
7. Beam Simply Supported at Ends – Concentrated load P at any point			
	$\theta_1 = \frac{Pb(l^2 - b^2)}{6EI}$ $\theta_2 = \frac{Pab(2l - b)}{6EI}$	$y = \frac{Pbx}{6EI} (l^2 - x^2 - b^2)$ for $0 < x < a$ $y = \frac{Pb}{6EI} \left[\frac{l}{b} (x - a)^3 + (l^2 - b^2)x - x^3 \right]$ for $a < x < l$	$\delta_{max} = \frac{Pb(l^2 - b^2)^{3/2}}{9\sqrt{3}EI}$ at $x = \sqrt{(l^2 - b^2)}/3$ $\delta = \frac{Pb}{48EI} (3l^2 - 4b^2)$ at the center, if $a > b$
8. Beam Simply Supported at Ends – Uniformly distributed load ω (N/m)			
	$\theta_1 = \theta_2 = \frac{\omega l^3}{24EI}$	$y = \frac{\omega x}{24EI} (l^3 - 2lx^2 + x^3)$	$\delta_{max} = \frac{5\omega l^4}{384EI}$
9. Beam Simply Supported at Ends – Couple moment M at the right end			
	$\theta_1 = \frac{Ml}{6EI}$ $\theta_2 = \frac{Ml}{3EI}$	$y = \frac{Mlx}{6EI} \left(1 - \frac{x^2}{l^2} \right)$	$\delta_{max} = \frac{Ml^2}{9\sqrt{3}EI}$ at $x = \frac{l}{\sqrt{3}}$ $\delta = \frac{Ml^2}{16EI}$ at the center
10. Beam Simply Supported at Ends – Uniformly varying load: Maximum intensity ω_0 (N/m)			
	$\theta_1 = \frac{7\omega_0 l^3}{360EI}$ $\theta_2 = \frac{\omega_0 l^3}{45EI}$	$y = \frac{\omega_0 x}{360EI} (7l^4 - 10l^2x^2 + 3x^4)$	$\delta_{max} = 0.00652 \frac{\omega_0 l^4}{EI}$ at $x = 0.519l$ $\delta = 0.00651 \frac{\omega_0 l^4}{EI}$ at the center
BEAM TYPE	SLOPE AT FREE END	DEFLECTION AT ANY SECTION IN TERMS OF x	MAXIMUM DEFLECTION
1. Cantilever Beam – Concentrated load P at the free end			
	$\theta = \frac{Pl^2}{2EI}$	$y = \frac{Px^2}{6EI} (3l - x)$	$\delta_{max} = \frac{Pl^3}{3EI}$
2. Cantilever Beam – Concentrated load P at any point			
	$\theta = \frac{Pa^2}{2EI}$	$y = \frac{Px^2}{6EI} (3a - x)$ for $0 < x < a$ $y = \frac{Pa^2}{6EI} (3x - a)$ for $a < x < l$	$\delta_{max} = \frac{Pa^2}{6EI} (3l - a)$
3. Cantilever Beam – Uniformly distributed load ω (N/m)			
	$\theta = \frac{\omega l^3}{6EI}$	$y = \frac{\omega x^2}{24EI} (x^2 + 6l^2 - 4lx)$	$\delta_{max} = \frac{\omega l^4}{8EI}$
4. Cantilever Beam – Uniformly varying load: Maximum intensity ω_0 (N/m)			
	$\theta = \frac{\omega_0 l^3}{24EI}$	$y = \frac{\omega_0 x^2}{120EI} (10l^3 - 10l^2x + 5lx^2 - x^3)$	$\delta_{max} = \frac{\omega_0 l^4}{30EI}$
5. Cantilever Beam – Couple moment M at the free end			
	$\theta = \frac{Ml}{EI}$	$y = \frac{Mx^2}{2EI}$	$\delta_{max} = \frac{Ml^2}{2EI}$

BFS 40103: ADVANCED STRUCTURE ANALYSIS

2) STIFFNESS MATRIX FORMULA

$$K = AE/L \begin{pmatrix} \lambda_x^2 & \lambda_x \lambda_y & -\lambda_x^2 & -\lambda_x \lambda_y \\ \lambda_x \lambda_y & \lambda_y^2 & -\lambda_x \lambda_y & -\lambda_y^2 \\ -\lambda_x^2 & -\lambda_x \lambda_y & \lambda_x^2 & \lambda_x \lambda_y \\ -\lambda_x \lambda_y & -\lambda_y^2 & \lambda_x \lambda_y & \lambda_y^2 \end{pmatrix}$$