

# UNIVERSITI TUN HUSSEIN ONN MALAYSIA

# FINAL EXAMINATION **SEMESTER I SESSION 2013/2014**

COURSE NAME

: STATISTICAL PACKAGES

COURSE CODE

: BWB 20703

PROGRAMME

: 2 BWQ

EXAMINATION DATE : DECEMBER 2013/JANUARY 2014

DURATION

: 3 HOURS

INSTRUCTION

A) ANSWER ALL (2)

**QUESTIONS IN SECTION A** 

B) ANSWER ONLY TWO (2) QUESTIONS IN SECTION B

THIS QUESTION PAPER CONSISTS OF TWENTY (20) PAGES

### **SECTION A**

Q1 (a) Two hundred and seventy nine Switzerland skiers were studied during two one-week periods in 1998. One group of 140 skiers receiving a placebo each day and the other 139 receiving one gram of ascorbic acid (known as Vitamin C) per day. The study was double blind - neither the subjects nor the researchers knew who received what treatment. Let  $p_1$  be the probability that a member of the ascorbic acid group contracts a cold during the study period and  $p_2$  be the corresponding probability for the placebo group. The researchers are interested in testing whether  $p_1 = p_2$ . The data are summarised as a two-by-two table of counts such as in the Table  $\mathbf{Q1(a)}$ .

TABLE Q1(a)

Outcome	Ascorbic Asid	Placebo
With cold	17	31
With no cold	122	109
Total	139	140

(i) Find the sample proportion of skiers developing colds in the placebo and treatment groups.

(4 marks)

(ii) Calculate the pooled proportion of the developed colds in the study.

(2 marks)

(iii) State and prove the hypothesis that the probability of contracting a cold is the different if given a placebo or Vitamin C at 5% level of significance.

(10 marks)

(iv) Find the 95% confidence interval of  $p_1 - p_2$  and state the appropriate conclusion.

(5 marks)

(b) The Minitab output of the cervical dysplasia data are as follows:

```
Test and CI for Two Proportions Sample X N Sample p 1 164 175 0.937143 2 130 308 0.422078 Difference = p (1) - p (2) Estimate for difference: 0.515065 95% CI for difference: (0.449221, 0.580909) Test for difference = 0 (vs not = 0): Z = 11.15 P-Value = 0.000
```

(i) Find the sample proportion of for Sample 1 and Sample 2. (2 marks)

(ii) State the hypothesis based on the output given above.

(2 marks)

- Q2 (a) A complementary subject for Bachelor student in UTHM have two tests and a final exam assessment. A linear regression model for the Final as response variable on Test 1 and Test 2 as explanatory variables for 24 students who took the subject were done as shown in the Appendix Q2. However, there was some argument whether the final exam assessment could reasonably be predicted from the two tests.
  - (i) What is the fraction of the variability in the Final is explained by the two tests?

(1 mark)

(ii) Give the fitted regression equation.

(1 mark)

(iii) From the results, it appears that one of the tests was more useful than the other in terms of predicting the Final. Which is the test? How do you know?

(2 marks)

(iv) Based on the output, find the correlation coefficient between Test 1 and Final. What is the correlation value?

(5 marks)

(v) The F value is given as 12.12. What hypothesis is being tested with this F value for this analysis? What conclusion do you reach about this hypothesis?

(3 marks)

(vi) Find the standard deviation of the Final. By using this value, make a conclusion as to whether the regression was useful.

(3 marks)

(b) Two groups of statisticians were surveyed regarding opinions as to the price of gold on December 31, 2012. These statisticians were either academic (major employment by college or university) or professional (major employment by bank or securities firm). The result could be seen in the Table Q2(b) below.

TABLE Q2(b)

Group	Number	Mean Average	Standard Deviation
Academic	24	250	40
Professional	30	210	30

The assumption made for this sample data population are equal standard deviations.

(i) Calculate the pooled standard deviation of the data above. (4 marks)

(ii) Find a 95% confidence interval for the population mean difference between these groups.

(6 marks)

### **SECTION B**

- Q3 (a) The question based on the data on the effect of Vitamin C on tooth growth in a group of rabbits. The variables are len, which is tooth length as a response variable, supp of which the levels are OJ (as orange juice) and VC (as ascorbic acid) and dose of the supplement in milligrams (0.5, 1.0 and 2.0) where R considers dose to be numerical. The result could be seen in the Appendix Q3.
  - (i) What is the command summary() for?
    (1 mark)
  - (ii) What is the object of this analysis? (1 mark)
  - (iii) Examine the number for object column and row. (2 marks)
  - (iv) How many variables involve in this object? (1 mark)
  - (v) What is the type of variable for supp? (1 mark)
  - (vi) What is the meaning of the R command below?
     ToothGrowth\$dose <- factor(ToothGrowth\$dose,
     levels=c(0.5,1.0,2.0),
     labels=c("low","med","high"))</pre>
    (2 marks)

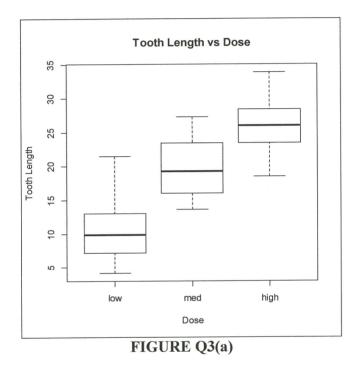
(vii) From the second summary(ToothGrowth), what is the most obvious result differ to previous summary(ToothGrowth) result?

(2 marks)

(viii) What is the meaning of R command below? ToothGrowth[seq(1,60,5),]

(2 marks)

(ix) Figure Q3(a) shows the plot of Tooth Length vs Dose. What is the R command should we use to plot the figure?



(3 marks)

- (b) From **Q3(a)**, the ANOVA test was run where two or more factor names separated by colons refer to the interaction between those factors.
  - (i) What is the obvious result could you interpret from the R command of summary (aov.out)?

(2 marks)

(ii) What is the model formula specifies by the R command below?

aov.out <- aov(len ~ supp \* dose, data=ToothGrowth)

(3 marks)

- (iii) What is the R command below mean?

  TukeyHSD(aov.out, which=c("dose"), conf.level=.99)

  (2 marks)
- (iv) Figure Q3(b) shows the plot of Tooth Length vs Supplement:Dose. What is the R command should we use to plot the figure?

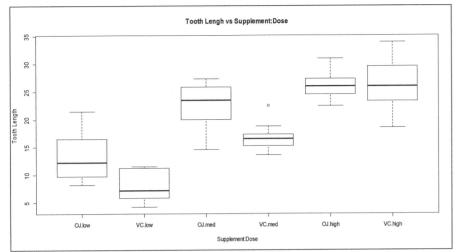


FIGURE Q3(b)

(3 marks)

- Q4 (a) The fish burger slices prepared by Kyros Kebab & Burger is supplied by a local fish packing factory known as Costcutter. The fish burger was ordered to the specification that each slice have a weight of 25 grams and contain no more than eleven grams of fat. The requirement that the weight be 25 grams is easily checked and there has never been a problem occurred. However, some concern that the fish burger slices might contain more than eleven grams of fat. The decision to do a quality control inspection was arrange for the random sampling of 80 fish burger slices where the fish burger slices had an average fat content of 14 grams, with a sample standard deviation of 1.2 grams.
  - (i) Calculate the t-statistic of the data given above. (4 marks)

State either **True** or **False** to each of the following questions (ii) to (vi).

(ii) This problem can be regarded as a test of the null hypothesis sample  $H_0: \mu = 11$ .

(1 mark)

(iii) The parameter  $\mu$  represents the mean weight of the 80 fish burger slices in the sample.

(1 mark)

(iv) The t statistic has 79 degrees of freedom.

(1 mark)

- (v) Most published t tables have no line for 79 degrees of freedom. (1 mark)
- (vi) At the 5% level of significance, one would accept the hypothesis in **Q4(a)(i)**.

(1 mark)

- (b) The marketing group in Alor Setar, Kedah plan to locate the regular drinkers of the Coke cans. The target population is defined for adults in the city of Alor Setar only. This is a situation of detecting events of low probability, as this is not a very popular drink.
  - (i) Suppose that 0.004 of the adults in Alor Setar are regular drinkers of Coke. What is the sample size should the marketing group use if they wants a probability of at least 80% of finding at least one Coke drinker in the sample?

(7 marks)

(ii) Suppose that 0.02 of the adults in Alor Setar are regular drinkers of Coke. What is the sample size should the marketing group use if they wants a probability of at least 80% of finding at least one Coke drinker in the sample?

(7 marks)

- (iii) Why an inequality direction reversed in the calculation above ? (2 marks)
- Q5 (a) The SPSS output is about the Maintenance System hire by one selected Mobile Company in Perak. By using the result given in the Appendix Q5, answer the following questions carefully.
  - (i) What is the proportion of participants are male?

(2 marks)

(ii) What is the frequency of respondents have lots of computer experience?

(1 mark)

	(iii)	What is the different percentage of the respondents was in IR experience and computer experience?	with some
		experience in IR experience and computer experience ?	(2 marks)
	(iv)	What is the missing terms refer in the SPSS Output given	? (1 mark)
	(v)	What is the percentage of the respondents were satisfied result?	
			(1 mark)
	(vi)	What is the proportion of the respondents were dissatisfied overall with the Maintenance System?	generally
			(2 marks)
	(vii)	How many respondents taken at most 14 minu Maintenance System?	tes using
		Maintenance System?	(2 marks)
(b)	packa works	nscombe dataset is one of the 102 available datasets age. The data in the datasets package are lazy losspace where no need to install the datasets package. Ba in Appendix Q5, answer each of the following questions.	ided in R sed on the
	(i)	How many variables in the object of anscombe?	(1 mark)
	(ii)	How many respondent in the anscombe dataset?	(1 mark)
	(iii)	Is there a linear relationship of the $x$ 's and the $y$ 's?	(1 mark)
	(iv)	What is the different of R command cor(ansco	mbe) and
		<pre>cor(anscombe[["x3"]],anscombe[["y2"]])?</pre>	(2 marks)
	(v)	What is the different of R command summary (ansc	ombe) and
		<pre>summary(anscombe)[,1:6]?</pre>	(3 marks)

(vi) What is the obvious different of the R command of the last summary (anscombe) from the previous summary (anscombe) in the output?

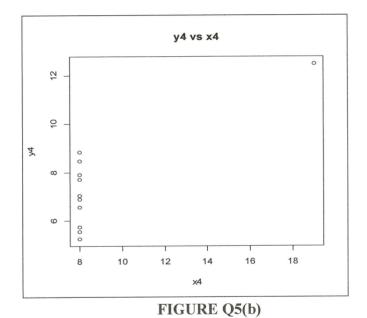
(2 marks)

(vii) What is the type of variables in the column four of the anscombe dataset?

(1 mark)

(viii) The Pearson correlation coefficient measures the strength of the linear relationship between two variables. Based on the Figure Q5(b), what is the type of relationship between two variables?What is the R command to plot the figure?

(3 marks)



- END OF QUESTION -

### FINAL EXAMINATION

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```
APPENDIX Q2
 data1 <- read.table("data1.txt",header=T)</pre>
> print(data1)
  Test1 Test2 Final
    110
        80 105
         102
              103
    110
3
              85
    75
         81
        108
             128
    118
              83
90
5
         33
    30
6
         64
   118
    59
         56 115
              79
75
8
    52
         78
9
    57
         69
         75 128
10
   105
111
    4.5
         42 106
        110
             155
12
   140
         65
              84
13
    47
  135
         80 120
14
15
    97
         95 132
        95 130
16
  100
         90 103
17
   100
         51 100
18
   32
         12
              45
19
    42
20 105
         99 121
        101 150
21
    60
    75
         77
               96
22
  125
23
        102
               150
24
    92
         91
              100
> names(data1)
[1] "Test1" "Test2" "Final"
> model1 <- lm(Final~Test1 + Test2,data=data1)</pre>
> summarv(model1)
Call:
lm(formula = Final ~ Test1 + Test2, data = data1)
Residuals:
        1Q Median 3Q
                           Max
  Min
-24.90 -14.83 -3.48 16.87 30.21
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 46.8453 12.9416 3.620 0.00161 **
           Test1
                     0.2299 2.811 0.01047 *
Test2
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' 1
Residual standard error: 18.95 on 21 degrees of freedom
Multiple R-squared: 0.5358, Adjusted R-squared: 0.4916
F-statistic: 12.12 on 2 and 21 DF, p-value: 0.0003162
> anova(model1)
Analysis of Variance Table
Response: Final
```

```
Df Sum Sq Mean Sq F value
                                        Pr(>F)
           1 5867.2 5867.2 16.3420 0.0005869 ***
Test1
          1 2836.7 2836.7 7.9012 0.0104705 *
Test2
Residuals 21 7539.6
                    359.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' 1
> names(data2)[4:5] <- c("Fits", "Residuals")
> print(data2)
                         Fits Residuals
   Test1 Test2 Final
           80 105 112.59986 -7.599855
     110
                103 126.81911 -23.819109
           102
     110
3
                 85 108.77630 -23.776300
     75
           81
                128 131.71878 -3.718776
83 72.00548 10.994523
4
    118
           108
5
            33
     30
                  90 103.28027 -13.280267
115 90.57468 24.425320
6
     118
            64
7
      59
            56
                 115
8
      52
            78
                  79 103.89996 -24.899958
                      98.72155 -23.721545
      57
            69
                  75
                 128 108.72965 19.270349
10
    105
            75
                      79.73811 26.261890
11
     45
            42
                 106
                 155 135.82108 19.178923
12
     140
           110
                  84 94.85912 -10.859116
13
      47
            65
                 120 115.79263
                                4.207370
14
     135
            80
                 132 120.63456 11.365442
15
      97
            95
                 130 121.01769
                                8.982309
16
            95
     100
                 103 117.78604 -14.786043
17
            90
     100
                 100 83.89483 16.105165
18
            51
      32
                  45 59.96508 -14.965085
19
            12
      42
20
                 121 124.24157 -3.241565
     105
            99
                 150 119.78723 30.212770
21
      60
           101
22
      75
            77
                  96 106.19098 -10.190981
                 150 128.73477 21.265226
23
     125
           102
                 100 117.41068 -17.410684
24
      92
            91
> # stem-and-leaf plot of the residuals
> stem(data2$Residuals,scale=2)
  The decimal point is 1 digit(s) to the right of the |
  -2 | 5444
  -1 | 755310
  -0 | 843
   0 | 49
   1 | 11699
   2 | 146
   3 | 0
```

### FINAL EXAMINATION

SEMESTER/SESSION: SEM I/2013/2014

COURSE NAME : STATISTICAL PACKAGES

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```
APPENDIX Q3
> data(ToothGrowth)
> str(ToothGrowth)
'data.frame': 60 obs. of 3 variables:
$ len : num 4.2 11.5 7.3 5.8 6.4 10 11.2 11.2 5.2 7 ...
$ supp: Factor w/ 2 levels "OJ", "VC": 2 2 2 2 2 2 2 2 2 2 ...
$ dose: num 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 ...
> dim(ToothGrowth)
[1] 60 3
> names(ToothGrowth)
[1] "len" "supp" "dose"
> print(ToothGrowth)
   len supp dose
       VC 0.5
  4.2
  11.5
        VC 0.5
  7.3
       VC 0.5
       VC 0.5
  5.8
       VC 0.5
  6.4
       VC 0.5
  10.0
       VC 0.5
  11.2
       VC 0.5
  11.2
        VC 0.5
  5.2
        VC 0.5
10 7.0
11 16.5
        VC 1.0
12 16.5
        VC 1.0
            1.0
13 15.2
         VC
            1.0
14 17.3
         VC
15 22.5
         VC
             1.0
16 17.3
         VC
             1.0
            1.0
17 13.6
         VC
            1.0
18 14.5
         VC
            1.0
19 18.8
         VC
            1.0
         VC
20 15.5
         VC 2.0
21 23.6
         VC 2.0
22 18.5
23 33.9
        VC 2.0
         VC 2.0
24 25.5
25 26.4
        VC 2.0
26 32.5
        VC 2.0
27 26.7
        VC 2.0
        VC 2.0
28 21.5
29 23.3
        VC 2.0
30 29.5
        VC 2.0
31 15.2
        OJ 0.5
32 21.5
        OJ 0.5
33 17.6 OJ 0.5
        OJ 0.5
34 9.7
35 14.5 OJ 0.5
```

```
36 10.0
        OJ 0.5
37 8.2
        OJ 0.5
38 9.4
        OJ 0.5
39 16.5
        OJ 0.5
40 9.7
         OJ
            0.5
41 19.7
         OJ
             1.0
             1.0
42 23.3
         OJ
43 23.6
             1.0
         OJ
44 26.4
         OJ
             1.0
45 20.0
         OJ
             1.0
46 25.2
         OJ
             1.0
47 25.8
         OJ
             1.0
            1.0
48 21.2
         OJ
         OJ 1.0
49 14.5
50 27.3
         OJ 1.0
         OJ 2.0
51 25.5
         OJ 2.0
52 26.4
         OJ 2.0
53 22.4
54 24.5
         OJ 2.0
55 24.8
         OJ 2.0
         OJ 2.0
56 30.9
         OJ 2.0
57 26.4
58 27.3
        OJ 2.0
59 29.4
       OJ 2.0
60 23.0 OJ 2.0
summary(ToothGrowth)
                           dose
           supp
Min. : 4.20 OJ:30 Min. :0.500
1st Qu.:13.07 VC:30 1st Qu.:0.500
Median :19.25
                       Median :1.000
Mean :18.81
                        Mean :1.167
3rd Qu.:25.27
                        3rd Qu.:2.000
Max. :33.90
                       Max. :2.000
> str(ToothGrowth)
'data.frame': 60 obs. of 3 variables:
$ len : num 4.2 11.5 7.3 5.8 6.4 10 11.2 11.2 5.2 7 ...
 $ supp: Factor w/ 2 levels "OJ", "VC": 2 2 2 2 2 2 2 2 2 2 ...
$ dose: num 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 ...
> dim(ToothGrowth)
[1] 60 3
> ToothGrowth$dose <-
factor(ToothGrowth$dose,levels=c(0.5,1.0,2.0),labels=c("low","med","hig
h"))
> str(ToothGrowth)
'data.frame': 60 obs. of 3 variables:
 $ len : num 4.2 11.5 7.3 5.8 6.4 10 11.2 11.2 5.2 7 ...
$ supp: Factor w/ 2 levels "OJ", "VC": 2 2 2 2 2 2 2 2 2 2 ...
 $ dose: Factor w/ 3 levels "low", "med", "high": 1 1 1 1 1 1 1 1 1 1 ...
summary(ToothGrowth)
                         dose
     len
               supp
 Min. : 4.20 OJ:30 low:20
 1st Qu.:13.07 VC:30 med :20
                        high:20
 Median:19.25
 Mean :18.81
 3rd Qu.:25.27
 Max. :33.90
```

```
> ToothGrowth[seq(1,60,5),]
  len supp dose
  4.2 VC low
10.0 VC low
16.5 VC med
6 10.0
11 16.5
16 17.3
         VC med
21 23.6
         VC high
        VC high
26 32.5
31 15.2
        OJ low
         OJ low
36 10.0
         OJ med
41 19.7
        OJ med
46 25.2
        OJ high
51 25.5
56 30.9 OJ high
replications(len~supp*dose,data=ToothGrowth)
    supp dose supp:dose
              20
                        10
      30
> replications(len~supp*dose,data=ToothGrowth[1:58,])
$supp
supp
OJ VC
28 30
$dose
dose
low med high
 20 20 18
$`supp:dose`
 dose
supp low med high
 OJ 10 10 8
 VC 10 10 10
> aov.out = aov(len ~ supp * dose, data=ToothGrowth)
> model.tables(aov.out, type="means", se=T)
Tables of means
Grand mean
18.81333
supp
supp
   oj vc
20.663 16.963
dose
dose
 low med high
10.605 19.735 26.100
 supp:dose
   dose
supp low med high
 OJ 13.23 22.70 26.06
  VC 7.98 16.77 26.14
```

```
Standard errors for differences of means
        supp dose supp:dose
       0.9376 1.1484 1.6240
         30 20
                          10
replic.
> summary(aov.out)
          Df Sum Sq Mean Sq F value
                                    Pr(>F)
            1 205.3 205.3 15.572 0.000231 ***
supp
           2 2426.4 1213.2 92.000 < 2e-16 ***
dose
                             4.107 0.021860 *
           2 108.3
                     54.2
supp:dose
         54 712.1
                       13.2
Residuals
Signif. codes: 0 \***' 0.001 \**' 0.01 \*' 0.05 \.' 0.1 \' 1
> TukeyHSD(aov.out, which=c("dose"), conf.level=0.95)
Tukey multiple comparisons of means
   95% family-wise confidence level
Fit: aov(formula = len ~ supp * dose, data = ToothGrowth)
$dose
                    lwr
                              upr padj
          diff
         9.130 6.362488 11.897512 0.0e+00
med-low
high-low 15.495 12.727488 18.262512 0.0e+00
high-med 6.365 3.597488 9.132512 2.7e-06
```

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## **APPENDIX Q5**

Gender of respondent

Gender of respondent						
		Frequency	Percent	Valid Percent	Cumulative	
					Percent	
	male	20	37.0	37.0	37.0	
Valid	female	34	63.0	63.0	100.0	
	Total	54	100.0	100.0		

IR experience

		Frequency	Percent	Valid Percent	Cumulative
					Percent
	none	3	5.6	5.6	5.6
	some	36	66.7	66.7	72.2
Valid	lots	15	27.8	27.8	100.0
	Total	54	100.0	100.0	

Computer experience

		Frequency	Percent	Valid Percent	Cumulative Percent
	some	34	63.0	63.0	63.0
Valid	lots	20	37.0	37.0	100.0
	Total	54	100.0	100.0	

Internet experience

		Frequency	Percent	Valid Percent	Cumulative
					Percent
	some	32	59.3	59.3	59.3
Valid	lots	22	40.7	40.7	100.0
	Total	54	100.0	100.0	

### Satisfaction with results

		Frequency	Percent	Valid Percent	Cumulative Percent
	dissatisfied	24	44.4	45.3	45.3
	neutral	15	27.8	28.3	73.6
Valid	satisfied	14	25.9	26.4	100.0
	Total	53	98.1	100.0	
Missing	missing	1	1.9		
Total		54	100.0		

General feelings overall

General techniqs over an					
		Frequenc	Percen	Valid Percent	Cumulative
		у	t		Percent
	dissatisfied	19	35.2	35.8	35.8
	neutral	18	33.3	34.0	69.8
Valid	satisfied	16	29.6	30.2	100.0
	Total	53	98.1	100.0	
Missing	missing	1	1.9		
Total		54	100.0		

**Photo Search** 

		Frequency	Percent	Valid	Cumulative
				Percent	Percent
	used	1	1.9	2.0	2.0
Valid	not used	50	92.6	98.0	100.0
	Total	51	94.4	100.0	
Missing	missing	3	5.6		
Total		54	100.0		

Time taken in minutes						
		Frequency	Percent	Valid Percent	Cumulative	
					Percent	
	1-4mins	1	1.9	2.1	2.1	
	5-9mins	11	20.4	22.9	25.0	
	10-14mins	7	13.0	14.6	39.6	
	15-19mins	13	24.1	27.1	66.7	
	20-24mins	6	11.1	12.5	79.2	
Valid	25-29mins	3	5.6	6.3	85.4	
	30-34mins	3	5.6	6.3	91.7	
	35-39mins	1	1.9	2.1	93.8	
	55-59mins	1	1.9	2.1	95.8	
	60-65mins	2	3.7	4.2	100.0	
	Total	48	88.9	100.0		
Missing	missing	6	11.1			
Total		54	100.0			

```
x1 x2 x3 x4 y1 y2 y3 y4
10 10 10 8 8.04 9.14 7.46 6.58
8 8 8 8 6.95 8.14 6.77 5.76
  13 13 13 8 7.58 8.74 12.74 7.71
  9 9 9 8 8.81 8.77 7.11 8.84
  11 11 11 8 8.33 9.26 7.81 8.47
  14 14 14 8 9.96 8.10 8.84 7.04
  6 6 6 8 7.24 6.13 6.08 5.25
  4 4 4 19 4.26 3.10 5.39 12.50
9 12 12 12 8 10.84 9.13 8.15 5.56
10 7 7 7 8 4.82 7.26 6.42 7.91
11 5 5 5 8 5.68 4.74 5.73 6.89
> class(anscombe)
[1] "data.frame"
> summary(anscombe)
                                         x4 y1
Min. : 8 Min. :
                                 хЗ
                   x2
 x1
             Min. : 4.0 Min. : 4.0
Min. : 4.0
4.260
                                                       1st Qu.:
                           1st Qu.: 6.5
                                          1st Qu.: 8
             1st Qu.: 6.5
1st Qu.: 6.5
6.315
                                                       Median:
                                          Median: 8
                           Median: 9.0
             Median: 9.0
Median: 9.0
7.580
                                          Mean : 9
                                                       Mean :
                           Mean : 9.0
             Mean : 9.0
Mean : 9.0
7.501
                                                       3rd Qu.:
                                          3rd Qu.: 8
              3rd Qu.:11.5 3rd Qu.:11.5
3rd Qu.:11.5
8.570
                                          Max. :19
                                                       Max.
             Max. :14.0 Max. :14.0
       :14.0
Max.
:10.840
```

> anscombe

```
уЗ
                                    y4
     y2
                                     : 5.250
               Min. : 5.39
                                Min.
     :3.100
Min.
                1st Qu.: 6.25
                                1st Qu.: 6.170
1st Qu.:6.695
Median :8.140
                Median: 7.11
                                Median : 7.040
                                Mean : 7.501
Mean :7.501
                     : 7.50
                Mean
                3rd Qu.: 7.98
                                3rd Qu.: 8.190
3rd Ou.:8.950
                                     :12.500
                     :12.74
                                Max.
Max. :9.260
                Max.
 summary(anscombe)[,1:6]
                                                        \times 4
                       x2
                                       xЗ
      x1
               " "Min.
                               " "Min. : 4.0 " "Min.
                                                         : 8
                       : 4.0
 "Min.
      : 4.0
                               " "1st Qu.: 6.5 " "1st Qu.: 8
               " "1st Qu.: 6.5
 "1st Qu.: 6.5
                                                               11
 "Median : 9.0 " "Median : 9.0
                               " "Median : 9.0 " "Median : 8
                                                               **
                               " "Mean : 9.0 " "Mean
               " "Mean : 9.0
 "Mean : 9.0
                                                               **
              " "3rd Qu.:11.5
                               " "3rd Qu.:11.5 " "3rd Qu.: 8
 "3rd Qu.:11.5
                       :14.0 " "Max. :14.0 " "Max.
                                                         :19
       :14.0 " "Max.
 "Max.
      у1
                         y2
        : 4.260 " "Min.
                           :3.100
 "Min.
 "1st Qu.: 6.315 " "1st Qu.:6.695
 "Median : 7.580 " "Median :8.140
 "Mean : 7.501 " "Mean
                         :7.501
 "3rd Qu.: 8.570 " "3rd Qu.:8.950
 "Max. :10.840 " "Max. :9.260
 cor(anscombe[["x1"]],anscombe[["y1"]])
[1] 0.8164205
 cor(anscombe[["x2"]],anscombe[["y2"]])
[1] 0.8162365
 cor(anscombe[["x3"]],anscombe[["y3"]])
[1] 0.8162867
 cor(anscombe[["x4"]],anscombe[["y4"]])
[1] 0.8165214
> cor(anscombe)
                                                                y2
                                                      y1
                                x3
                                           \times 4
                     x^2
          x1
у3
k1 1.0000000 1.0000000 1.0000000 -0.5000000 0.8164205 0.8162365
0.8162867
                        1.0000000 -0.5000000 0.8164205 0.8162365
x2 1.0000000
              1.0000000
0.8162867
k3 1.0000000 1.0000000 1.0000000 -0.5000000 0.8164205 0.8162365
0.8162867
k4 -0.5000000 -0.5000000 -0.5000000 1.0000000 -0.5290927 -0.7184365 -
0.3446610
\sqrt{1} 0.8164205 0.8164205 0.8164205 -0.5290927 1.0000000 0.7500054
0.4687167
\sqrt{2} 0.8162365 0.8162365 0.8162365 -0.7184365 0.7500054 1.0000000
0.5879193
y3 0.8162867 0.8162867 0.8162867 -0.3446610 0.4687167 0.5879193
1.0000000
\sqrt{4} -0.3140467 -0.3140467 -0.3140467 0.8165214 -0.4891162 -0.4780949 -
0.1554718
```

```
x1 -0.3140467
x2 -0.3140467
x3 -0.3140467
x4 0.8165214
y1 -0.4891162
y2 -0.4780949
y3 -0.1554718
y4 1.0000000
> summary(anscombe)
  x1
                                                y1
Min. : 4.260
                          x3 x4
Min. : 4.0 yes:10
                                         \times 4
                  x2
             Min. : 4.0
Min. : 4.0
                           1st Qu.: 6.5 no : 1
                                                1st Qu.: 6.315
Median : 7.580
                          Median: 9.0
                          Mean : 9.0
                                                Mean : 7.501
             Mean : 9.0
 Mean : 9.0
                                                3rd Qu.: 8.570
              3rd Qu.:11.5 3rd Qu.:11.5
 3rd Qu.:11.5
 Max. :14.0 Max. :14.0 Max. :14.0
                                                Max. :10.840
              y3
Min. : 5.39
                           y4
Min. : 5.250
 y2
Min. :3.100
              1st Qu.: 6.25
                           1st Qu.: 6.170
 1st Qu.:6.695
             Median : 7.11
                           Median : 7.040
 Median :8.140
 Mean :7.501
              Mean : 7.50 Mean : 7.501
 3rd Qu.:8.950 3rd Qu.: 7.98 3rd Qu.: 8.190
 Max. :9.260 Max. :12.74 Max. :12.500
```