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Universiti Tun Hussein Onn Malaysia

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
(ONLINE)
SEMESTER II
SESSION 2019/2020**

COURSE NAME : CIVIL ENGINEERING
MATHEMATICS III

COURSE CODE : BFC 24103

PROGRAMME CODE : BFF

EXAMINATION DATE : JULY 2020

DURATION : 6 HOURS

INSTRUCTION : ANSWER ALL QUESTIONS

THIS QUESTION PAPER CONSISTS OF **FOUR (4)** PAGES

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- Q1** (a) Solve $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2+y^2}{\sqrt{x^2+y^2+1}-1}$. (6 marks)
- (b) Find f_x, f_y, f_{xx}, f_{xy} for function $f(x, y) = y \tan 2x$. (8 marks)
- (c) Evaluate $\int_0^1 \int_0^{\sqrt{1-x^2}} x + y \, dydx$ by using polar coordinates. (6 marks)
- Q2** (a) Calculate the volume of solid bounded by $y = x^2 + z^2$ and plane $y = 3$ in first octant by using triple integral. (5 marks)
- (b) A cylinder with diameter 12 cm and height 14 cm was used to collect the sample of peat soil. Determine the rate of change in a cylinder if the increasing rate of radius is 0.3 cms^{-1} and the decreasing rate of height is 0.4 cms^{-1} . (4 marks)
- (c) Given that $r(t) = e^t \mathbf{i} + 2\sin t \mathbf{j} + 2\cos t \mathbf{k}$. Find the velocity and acceleration at $t = \pi$. (6 marks)
- (d) Find a parametric equation of the line through the points A (4,5,-3) and B (6,-5,4). (5 marks)
- Q3** (a) Solve $\int_0^1 \int_x^1 xy^3 \, dydx$. (5 marks)
- (b) The demand equation for a certain brand of face mask for front liners used during MCO is $k = 2xy^2z^3$ where x represents the time of face mask needed to be supplied in a month. The price of the facemask, y is given by the equation $y = x^2 + 1$ with the types of brand face mask, $z = \sqrt{x}$. Determine the quantity of the face mask needed to be supplied in a month, $\frac{dk}{dx}$ using the appropriate rule method. (5 marks)
- (c) Ukur Bina Sdn Bhd is awarded a survey work for Perwira residential apartment. As a surveyor, you are required to conduct surveying to set out the exact position of a proposed structure within the legal boundaries. The setting out works is bounded at $y = 2x$, $y = \frac{x}{2}$ and $x + y = 3$. With the aid of reference equations, sketch the bounded boundaries. (8 marks)

- (d) A particle describes a path in which its position vector, $r(t)$, is given a function of time, t , by $r(t) = 3t \mathbf{i} + 4\sin t \mathbf{j} + 4\cos t \mathbf{k}$ where \mathbf{i} , \mathbf{j} and \mathbf{k} are three mutually perpendicular unit vectors. Calculate the unit tangent vector, principal unit normal vector and curvature of the particle.

(12 marks)

- Q4** (a) (i) Sketch the region R enclosed between the line $y = \frac{x}{2}$, $y = 2x$ and $x + y = 3$.
(4 marks)
- (ii) Find the area of region R using double integrals.
(6 marks)
- (b) Calculate the directional derivatives of functions $f(x, y) = 4x^3y^2$ at point (2,1) in the direction of vector $\mathbf{a} = 4\mathbf{i} - 3\mathbf{j}$.
(6 marks)
- (c) Find the line integral using Green's theorem $\oint_C y^3 dx + (x^3 + 3xy^2) dy$ where C is the boundary of circle $x^2 + y^2 = 9$ which oriented counter clockwise.
(14 marks)

- END OF QUESTIONS -

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Formulae

Tangent Plane: $z - z_0 = f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0)$

Polar coordinate: $x = r \cos \theta, y = r \sin \theta, \theta = \tan^{-1}(\frac{y}{x})$ and

$$\iint_R f(x, y) dA = \iint_R f(r, \theta) r dr d\theta$$

Cylindrical coordinate: $x = r \cos \theta, y = r \sin \theta, z = z, \iiint_G f(x, y, z) dV = \iiint_G f(r, \theta, z) r dz dr d\theta$

Spherical coordinate. $x = \rho \sin \phi \cos \theta, y = \rho \sin \phi \sin \theta, z = \rho \cos \theta, x^2 + y^2 + z^2 = \rho^2, 0 \leq \theta \leq 2\pi, 0 \leq \phi \leq \pi$ and $\iiint f(x, y, z) dV = \iiint f(\rho, \phi, \theta) \rho^2 \sin \phi d\rho d\phi d\theta$

Directional derivative: $D_u f(x, y) = (f_x \mathbf{i} + f_y \mathbf{j}) \cdot u$

Let $\mathbf{F}(x, y, z) = M\mathbf{i} + N\mathbf{j} + P\mathbf{k}$ is vector field, then the divergence of $\mathbf{F} = \nabla \cdot \mathbf{F} = \frac{\partial M}{\partial x} + \frac{\partial N}{\partial y} + \frac{\partial P}{\partial z}$

The curl of

$$\nabla \times \mathbf{F} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ M & N & P \end{vmatrix} = \left(\frac{\partial P}{\partial y} - \frac{\partial N}{\partial z} \right) \mathbf{i} - \left(\frac{\partial P}{\partial x} - \frac{\partial M}{\partial z} \right) \mathbf{j} + \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) \mathbf{k}$$

Let C is a smooth curve given by $\mathbf{r}(t) = x(t)\mathbf{i} + y(t)\mathbf{j} + z(t)\mathbf{k}, t$ is parameter, then

The unit tangent vector; $\mathbf{T}(t) = \frac{\mathbf{r}'(t)}{\|\mathbf{r}'(t)\|}$

The unit normal vector: $\mathbf{N}(t) = \frac{\mathbf{T}'(t)}{\|\mathbf{T}'(t)\|}$

The binormal vector: $\mathbf{B}(t) = \mathbf{T}(t) \times \mathbf{N}(t)$

The curvature: $K = \frac{\|\mathbf{T}'(t)\|}{\|\mathbf{r}'(t)\|} = \frac{\|\mathbf{r}' \times \mathbf{r}''(t)\|}{\|\mathbf{r}'(t)\|^3}$

Green Theorem: $\oint_C M(x, y) dx + N(x, y) dy = \iint_R \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dA$